The 'Portuguese School of Extremes and Applications' (PORTSEA)

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The 'School of Extremes' in Portugal is nowadays well recognized by Abstract: the international scientific community. This recognition is mainly due to the scientific work of Tiago de Oliveira in the area. But I also need to mention the research developed by myself and Feridun Turkman in the field, while working for PhD in Sheffield, United Kingdom, and the organization of a NATO Advanced Study Institute (ASI) on Statistical *Extremes and Applications* (SEA), which took place at Vimeiro in the summer of 1983. Indeed, the organization of this 1983 NATO ASI (SEA 1983) was a landmark for the international recognition of the group and the launching of what I dare to call the Portuguese School of Extremes and Applications (PORTSEA). It is still sensible to refer that Laurens de Haan, one of the giants in the area of *Extremes*, came to Portugal in 1999, becoming then a member of the 'Centro de Estatística e Aplicações', the main pole of development of *Extremes* in Portugal, and consequently a member of the PORTSEA. The dynamic of publication has been very high, and I consider it quite above the average of our international partners. The topics under investigation in the area of *Extremes* are quite diverse. Apart from a large group working in the area of Parametric, Semi-parametric and Non-parametric Estimation of Parameters of Rare Events, the PORTSEA has strong groups in Univariate, Multivariate, Multidimensional and Spatial Extremes. We thus think that the dynamism of the Group will provide a healthy growing of the field, with a high international recognition of a 'School of Extremes in Portugal, a country of 'good extremists' in an extreme of Europe.

1 The beginning of PORTSEA

After getting an undergraduate degree in *Pure Mathematics (Algebra)*, in 1970, at "*Faculdade de Ciências da Universidade de Lisboa*" (FCUL), I took the decision to go on with research in the area of *Probability, Statistics and Stochastic Processes*. I became then a member of the *Statistics* group, and began working at "*Departamento de Matemática*", FCUL, in the field of *Non-parametric Methodologies*, under

the supervision of Professor José Tiago da Fonseca Oliveira (Tiago de Oliveira), already a prominent international reference in the area of *Statistics of Extremes and Applications* (SEA), with several articles in the area since 1959.

During the period I worked in Portugal as a research assistant, first at "Centro de Matemática Aplicada", and next at "Centro de Estatística e Aplicações da Universidade de Lisboa" (CEAUL), a Research Centre founded in 1975 by Tiago de Oliveira, and despite the fact that I had not so far worked in the field of Extreme Value Theory (EVT), I was well acquainted with the potentialities and beauty of EVT.

The investment policy inspired by Veiga Simão, a true reformer of Higher Education in Portugal, opened up great prospects for researchers considered promising, who were sent to major cultural centres abroad. My husband, Dinis Pestana, and I got a Calouste Gulbenkian fellowship and were accepted at the University of Sheffield, *United Kingdom* (UK), where Joe Gani had created the *Applied Probability Trust*, still responsible for the publication of two of the main journals in *Probability* (*Journal of Applied Probability* and *Advances in Applied Probability*).

Taken the decision of going to Sheffield, UK, for PhD, in the area of *Non*parametric Statistics, possibly under the supervision of Joe Gani, a friend of Tiago de Oliveira, I met Clive Anderson, who had finished his PhD thesis in 1971 in the field of *Extremes*, at the *Imperial College of London*, and who was well acquainted with the work of Tiago de Oliveira. Clive turned out to be my PhD supervisor, and from the beginning of 1976 onwards I began doing research 'almost full-time' in the field of *Extremes*.

Working also for PhD in Sheffield, in a related area, but under the supervision of Morris Walker, was Kamil Feridun Turkman, now Full Professor (already retired) of the "Departamento de Estatística e Investigação Operacional" (DEIO), and Antónia Amaral (now Antónia Amaral-Turkman), a colleague and friend of mine at FCUL, who began working for PhD by the end of 1977, also in Sheffield, but in the area of Bayesian Statistics, under the supervision of Ian Dunsmore.

SEA was then (and it is still now ...) considered as a quite relevant area in the field of *Statistics*, with a lot of topics to be exploited. Indeed, in the first decades of the twentieth century, under the powerful influence of Paul Lévy, *Probability Theory* was mainly concerned with generalizations of the *Central Limit Theorem* (CLT), related to the asymptotic behaviour of sums—a problem of great importance, since averages, variances and many other relevant statistics are simple sum functions. But Fréchet, in 1927, had the interesting idea of using an analogue of the Lévy stability equation for sums, just noticing that the maximum of maxima is still a maximum. He then just replaced powers of characteristic functions by powers of distribution functions, that is, he treated a problem analogous to that of sums, but for maxima

of independent, identically distributed random variables. He thus came to the first law of extremes, rightly called Fréchet distribution, with a functional form of the type

$$\Phi_{\alpha}(x) = \exp(-x^{-\alpha}), \ x \ge 0 \quad (\alpha > 0)$$

At the same time, Fisher and Tippett, in 1928, discovered the three types of solutions to which the max-stability equation can lead,

Type I (Gumbel) :	$\Lambda(x) = \exp(-\exp(-x)), \ x \in \mathbb{R},$
Type II (Fréchet) :	$\Phi_{\alpha}(x) = \exp(-x^{-\alpha}), \ x \ge 0 (\alpha > 0),$
Type III (max-Weibull) :	$\Psi_{\alpha}(x) = \exp(-(-x)^{\alpha}), \ x \le 0 (\alpha > 0).$

Meanwhile, von Mises, in 1936, proposed an expression encompassing these three laws,

$$G(x) \equiv G_{\xi}(x) := \begin{cases} \exp\left(-(1+\xi x)^{-1/\xi}\right), \ 1+\xi x > 0, & \text{if } \xi \neq 0, \\ \exp(-\exp(-x)), \ x \in \mathbb{R}, & \text{if } \xi = 0. \end{cases}$$

Indeed, with $\xi = 0$, $\xi = 1/\alpha > 0$ and $\xi = -1/\alpha < 0$, respectively, we have $\Lambda(x) = G_0(x)$, $\Phi_\alpha(x) = G_{1/\alpha}(\alpha(1-x))$ and $\Psi_\alpha(x) = G_{-1/\alpha}(\alpha(x+1))$. Currently (for more details, see the reasonably recent overview by Gomes and Guillou, 2015), these results are unified in a general theory, which recognizes that the *Extremal Types Theorem* (ETT) and other ETT generalizations are a reference for the study of extreme order statistics, while the CLT has to do with sums and central order statistics.

A little later, statistical EVT had a strong development under the vigorous impulse of Emil Julius Gumbel, in the late sixties. And the *School of Extremes* (and *Risk Evaluation*) in Portugal, or the '*Portuguese School of Extremes and Applications*' (PORTSEA), is nowadays well recognized by the international scientific community, And such a recognition is mainly due to the scientific work of Tiago de Oliveira, Effective Member of the '*Academia das Ciências de Lisboa*' (ACL) from 1985 until his premature death in 1992.



Figure 1: José Tiago da Fonseca Oliveira (1928-1992), with his famous pipe

But I also need to mention the research developed by myself and by Kamil Feridun Turkman in the field, while working for PhD in Sheffield, United Kingdom, in the late seventies—early eighties.

I got the PhD degree by the end of 1978 (Gomes, 1978), under the supervision of Clive Anderson, an eminent scientist in the field of *Extremes*. Dinis Pestana, my husband, also got his PhD in Sheffield, in 1978, in topics related to sums of random variables, under the supervision of Damodar N. Shanbhag. We both came then back to FCUL in 1979, and collaborated actively in the foundation in 1980 of the "*Sociedade Portuguesa de Estatística e Investigação Operacional*" (SPEIO), with Tiago de Oliveira as the first President. SPEIO was profoundly restructured in 1991, with the current designation "*Sociedade Portuguesa de Estatística*" (SPE), and has had a big impact in the development of *Statistics* in Portugal. I myself was the first President of SPE (1990-1994), followed by João A. Branco (1994-2000), Fernando Rosado (2000–2006), Carlos Braumann (2006–2012), Carlos D. Paulino (2012–2015), Maria Eduarda Silva (2015–2020), and now, since the beginning of 2021, Miguel de Carvalho, a researcher with a lot of work in the field of *Extremes* and who I also consider as a member of PORTSEA.

In 1981, and after getting his PhD in 1980 (Turkman, 1980), also in Sheffield, in the area of *Extremes in Stochastic Processes* and under the supervision of Morris Walker, Feridun Turkman joined us at FCUL and at the '*Centro de Estatística e Aplicações da Universidade de Lisboa*' (CEAUL), the main pole of development of *Extremes* in Portugal. Antónia Amaral-Turkman, Dinis Pestana, Feridun Turkman and I, Ivette Gomes, together with Cristina Sernadas (also from *Statistics*) and colleagues from *Operations Research* (J. Dias Coelho) and *Computing* (Amílcar Sernadas), all young people who had also got their PHDs abroad, worked hard, jointly with Tiago de Oliveira, in the foundation, in 1981, of the "*Departamento de Estatística, Investigação Operacional e Computação*" (DEIOC), now DEIO, with the first degrees in the area of *Statistics*, in Portugal, one in *Probability and Statistics* and another one in *Statistics and Operations Research*.

In the mid of 1981, after the formation of DEIOC, Feridun and I, jointly with Tiago de Oliveira, have proposed the organization of a NATO Advanced Study Institute (ASI) on SEA, which took place at Vimeiro in the summer of 1983 (SEA 1983). As already mentioned here, and also in Gomes (2005, 2007), two articles written in Portuguese, at SPE Bulletin, the development of the 'School of Extremes' in Portugal undoubtedly had as its main responsibility the scientific work of Tiago de Oliveira in the area. But the organization of the 1983 NATO ASI was indeed a landmark for the international recognition of the group. Although they have not usually been considered as elements of this group, due to the fact that their main topics of research are not in the field of Extremes, I am sure that Antónia Amaral-Turkman and Dinis Pestana have also played a significant role in the construction of the group, even co-authoring several relevant articles in this area. Indeed, the ASI on SEA had the three aforementioned organizers, but also two 'shadow organizers', Antónia and Dinis, whom I also consider as members of the PORTSEA, and who are also pictured in Figure 2.



Figure 2: Organizers (top) and shadow organizers (bottom) of the NATO ASI on Statistics of Extremes and Applications (SEA 1983)

2 SEA 1983 and the launching of PORTSEA

The SEA 1983 NATO ASI was held in Vimeiro, from 31st of August until September 14, and had the participation of prominent researchers in the area, with some of them present in the photo provided in Figure 3.



Figure 3: Photo of NATO ASI participants—Vimeiro (SEA 1983)

Among those participants, I mention the invited foreign speakers, Clive Anderson (Sheffield University, UK), Paul Deheuvels (Université Paris VI, France), Benjamin Epstein (Technion, Israel), Janos Galambos (Temple University, USA), Arne Fransén (National Defence Research Institute, Sweden), Laurens de Haan (Erasmus University of Rotterdam, The Netherlands), Leon Herbach (Polytechnic Institute of New York, USA), A.M. Hasofer (University of New South Wales, Australia), Ross Leadbetter (University of North Carolina, USA), Georg Lindgren (University of Lund, Sweden), Nancy Mann (Department of Biomathematics, UCLA, USA), B. Marcus (Texas A&M University, USA), Yashaswini Mittal (Virginia Polytechnic Institute and State University, USA), James Pickands III (University of Pennsylvania, USA), Sid Resnick (Colorado State University, USA), Holger Rootzén (University of Copenhagen and UNC, Chapel Hill, USA), G.A. Schuëller (Institut fur Mechanik, Universitat Innsbruck, Austria), Masaaki Sibuya (Keio University, Japan), R. Sneyers (Royal Meteorological Institute, Brussels), Jef Teugels (Katholieke Universiteit Leuven, Belgic), Ishay Weissman (Technion, Israel), Vujica Yevjevich (International Water Resources Institute, George Washington University, USA).

Also, some of the students of the first DEIOC MSc course on *Probability and Statistics*, like Teresa Alpuim, Emília Athayde, Isabel Barão and Fátima Miguéns, as well as Fernando Rosado, a PhD student of Tiago de Oliveira and two PhD students of Dinis Pestana, Eugénia Graça Martins and Helena Iglésias Pereira, were young participants of this ASI. And in the list of authors of '*contributed papers*' we can find names of giants in the area of *Extreme Value Analysis* (EVA), like Richard Davis, Anthony Davison, Jürg Hüsler, Rolf Reiss, Richard Smith ...

As mentioned above, this NATO ASI on SEA is currently recognized as a milestone in the area of EVA. And repeating again what I said before in several occasions (see, for instance, the interviews in Fraga Alves and De Carvalho, 2015; Freitas ACM and Freitas JM, 2018), it was indeed true that when Richard Davis, one of the organizers of EVA 2009 (The Sixth International Conference on Extreme Value Analysis), which was held at Fort-Collins, Colorado, USA, spoke about Vimeiro's meeting as EVA-0, and when I read at EVA 2013 website: 'It has been 30 years since the socalled zero-th EVA conference took place in 1983 in Vimeiro, a small town near the beach in Portugal' ... I indeed felt some 'Nostalgia' ...



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In the Preface of the book associated with this NATO ASI, edited by Tiago de Oliveira (Tiago de Oliveira, Ed., 1984a) and dedicated to the memory of Emil Julius Gumbel, one of the pioneers in *Statistics of Extremes*, and a scientist with whom Tiago de Oliveira collaborated in the sixties, at Columbia University, one can find articles written by the aforementioned prominent researchers. In such a Preface we can read: '... the narrow and shallow stream (of extremes) gained momentum and is now a huge river, enlarging at every moment and flooding the margins'. And Tiago de Oliveira ends the Preface with thanks to the members of the recently formed DEIOC/FCUL, now DEIO/FCUL, saying: '... it is a very good group that crossed the desert during the organization time and continues to work on...'

The urge to publish was then reduced. In reality, two of the most relevant results contained in my 1978 thesis,

- the derivation of the joint distribution of upper order statistics and their concomitants, or induced order statistics,
- and the study of rates of convergence and penultimate or pre-asymptotic behaviour of sequences of extremes,

were published only in 1981 and in 1984 (Gomes, 1981a; 1984c), respectively. This second result clarified an issue raised by Sir Ronald Fisher and Leonard Tippett, in their seminal 1928 article. And the clarification of an issue that over 50 years had been addressed with limited success by several experts, put me on the attention radar of some of the gurus in the area, namely Herbert David, Janos Galambos, Laurens de Haan, Ross Leadbetter, all participants of SEA 1983. And this topic has continued and still bears fruit, with recent applications to the reliability of high-dimension coherent systems (see Reis *et al.*, 2015, among other papers).

However, in the 10-years period, 1975–1984, and including 'almost all' published material in the field of *Extremes* by the Portuguese community, I could count **43** publications (Fransén and Tiago de Oliveira, 1984; Gomes, 1978, 1979a,b, 1980a,b, 1981a,b, 1982, 1984a,b,c,d,e; Gomes and Pestana, 1978, 1981a,b; Iglésias Pereira, 1983; Tiago de Oliveira, 1975, 1977a,b,c, 1978a,b, 1981, 1982a,b,c,d, 1983, 1984a,b,c,d,e; Tiago de Oliveira and Epstein, 1982; Tiago de Oliveira and Gomes, 1984; Turkman, 1980, 1982, 1984a,b; Turkman and Walker, 1983, 1984), but **20** of them (around 47%) were coauthored by Tiago de Oliveira.

In that distant 1983, the community of 'extremists' was just emerging. There were **15** days of intense exchange of ideas, which renewed my enormous enthusiasm for EVT. And EVT has developed rapidly in recent decades due to its importance in the assessment of catastrophic risks in the most diverse human activities, among which I mention, *Economy, Finance, Health, Industry, Insurance* and *Population Dynamics*. EVT is essential for the construction of large structures in which it is necessary to assess levels of exceedance, for example of wind speeds or of river flows during floods. And it is one of the instruments of research in *Climatology, Energy, Environment, Hydrology* —in short, EVT has invaded almost all fields of science and technology related to a collective survival, where parameters of rare events are relevant. That is why we welcome the important international impact of Portuguese '*extremism*', whose success is bound to be increasingly visible.

At the time, research in mathematics was usually more solitary than it is today. The fashion for international collaborations was not yet in place. Anyway, the publication of research together with Martin van Montfort, from Wageningen University (van Montfort and Gomes, 1985; Gomes and van Montfort, 1986), and my collaboration with Laurens de Haan, from the Erasmus University of Rotterdam, were certainly auspicious consequences of this long congress. Regarding joint publications with Laurens de Haan, I am merely referring to the editions of books associated with international conferences organized by us (Gomes *et al.*, Eds., 2003; Fraga Alves *et al.*, Eds., 2007b, 2011) and the articles in international peridicals (Gomes and de Haan, 1999; Gomes *et al.*, 2002, 2004b, 2006, 2008c; Fraga Alves *et al.*, 2003, 2007a, 2009).

I now dare to say again (see, Gomes, 2005, 2007, 2013b, 2017) that the organization of the 1983 NATO ASI (or SEA 1983), with two Wednesday's afternoons and two whole weekends, full of social program, under my responsibility, despite of a bit 'traumatizing', in such a way that only after 1999 did I advance with the organization of conferences in Portugal, was indeed a landmark for the international recognition of the group and the launching of the PORTSEA, with an active life of almost 40 years, if we count it only after 1983.

With some work in the area of *Extremes*, although slight collateral to the subject of their PhD, I also mention Eugénia Graça Martins, with a PhD thesis discussed in 1983, and Helena Iglésias Pereira, who got her PhD degree at FCUL, in 1985, both supervised by Dinis Pestana. In the area of *Risk and Ruin Theory*, which can potentially be partially included in PORTSEA, something '*I hope for the future*', I mention Lurdes Centeno and Alfredo Egídio dos Reis, who got their PhD Degrees in 1985 and 1994 respectively, at Heriot-Watt University (UK), and who are now Full Professors at *Instituto Superior de Economia e Gestão* (ISEG).

In the meantime, Margarida Brito (University of Porto), who obtained her PhD degree in the area of *Extremes* at the University of Paris VI (Brito, 1987), under the supervision of Paul Deheuvels, came back to Portugal, being now an Associate Professor at O'Porto University. Prior to her PhD, she was already author of an article at an international periodical (Brito, 1986).

From the beginning of the 1980s, the investment policy inspired by Veiga Simão began to bear fruit, in the sense that a few groups with a reasonable critical mass were created here in Portugal. And, together with a few PhDs got in the best centres out of Portugal, those groups allowed the beginning of a '*banal*' supervision of PhD's in Portugal, together with PhDs obtained in the best foreign centres. I next sequentially mention the different PhD thesis:

— The first student to get a PhD degree in Portugal fully in the area of *Extremes* was Teresa Alpuin, now Full Professor at DEIO. She got her PhD degree in 1989, under my supervision, at *Universidade de Lisboa* (Alpuin, 1989). Her

thesis gave rise to seminal papers in the field of *Extremes for Dependent Se*quences, among which I refer only the three articles published prior to her PhD (Alpuin, 1986, 1988; Gomes and Alpuin, 1986), a record perhaps difficult to overpass ...

- Almost simultaneously, but already in 1990, Manuela Neves (Neves, 1990), now Full Professor at the 'Instituto Superior de Agronomia' (ISA), 'Universidade Técnica de Lisboa' (UTL), now ULisboa, defended her PhD thesis, at 'Universidade Nova de Lisboa' (UNL), under the supervision of Tiago de Oliveira. She was thus the first PhD student of Tiago de Oliveira in the field of Extremes.
- Also pioneers in this area are my second and third PhD students, Luísa Canto e Castro and Isabel Fraga Alves, who defended their PhD theses in 1992 (Canto e Castro, 1992; Fraga Alves, 1992a). Prior to their PhD, they have also published articles in international periodicals (Canto e Castro, 1987; Fraga Alves, 1992b).
- Fernanda Oliveira defended her PhD thesis also in 1992 (Oliveira MF, 1992), under the supervision of Feridun Turkman. Prior to her PHD, she had two publications at international periocicals (Oliveira MF and Turkman, 1992; Turkman and Oliveira MF, 1992).
- Although in a collaborative way, I also consider Nuno Crato, who got his PhD degree at the University of Delaware (Crato, 1992), USA, under the guidance of Howard Taylor, being now a Full Professor at ISEG, as a pioneering name for the development of what I dare today to call the 'School of Extremes in Portugal'.
- Professor Tiago de Oliveira only quite late decided for the supervision of PhD students in his most relevant area of research, and unfortunately, due to his premature death in 1992, when he was 63 years old, he has only seen the discussion of Manuela Neves' PhD thesis. Two other PhD students of Tiago Oliveira, in the area of *Extremes*, and members of DEIO/FCUL, Isabel Barão and Teresa Themido Pereira, have finished their PhD thesis, already under my supervision (Barão, 1993; Themido Pereira, 1994).
- Also in 1994, Emília Athayde (Athayde, 1994) at FCUL, and Helena Ferreira (Ferreira H, 1994) at the University of Coimbra, got PhD degrees under my supervision. Emília Athayde managed to have a book chapter published prior to the obtention of her PhD degree (Athayde and Gomes, 1987) and an article in a reputed international periodical (Alpuim and Athayde, 1990). And Helena Ferreira published an article in a highly reputed international journal (Ferreira H, 1993), prior to the obtention of her PhD degree.

This was the beginning of the Portuguese '*extremism*'. First under the direct guidance of the aforementioned researchers, and next by the scientific 'grandchildren'

and 'great-granchildren' of initial members, was created the PORTSEA, recognized internationally, whose members are spread throughout all Portuguese universities, and even around the world. For some, the passage through the universe of *Extremes* was fleeting, directing their interests to other areas, but most of the researchers who got their PhD in the area continued to publish firmly in the wide range of EVA, and many others whose usual research activities are developed in other areas have occasionally produced valuable work in the field of *Extremes*.

3 The growth of PORTSEA—Further PhD Thesis and Habilitation Degrees

From the beginning of 1994 and until the end of 2003, in a period of 10 years, the PhDs of Portuguese researchers in the area of *Extremes* have followed at a quite interesting rhythm. And apart from the **3** aforementioned PhD thesis written by Teresa Themido Pereira, Emília Athayde and Helena Ferreira, in 1994, **16** additional PhD thesis were mentioned in Gomes (2005):

- One of my MSc students, João Gomes (Gomes J, 1996), worked under the supervion of M. Teresa Alpuin, being thus my first scientific 'grandson'.
- Under my supervision, it is possible to count three additional thesis, in this period, written by M. Adelaide Valente de Freitas (Valente de Freitas, 1998), Andreia Hall (Hall, 1998) and Orlando Oliveira (Oliveira O, 2003). Regarding publications prior to their PhDs, I refer Hall (1996), Gomes J and Oliveira O (1997), Gomes MI and Oliveira O (2001).
- Fátima Brilhante (Brilhante, 1999) and Sandra Mendonça (Mendonça, 2001) worked under the supervision of Dinis Pestana.
- M. Graça Temido (Temido, 2000) worked under my co-supervision, jointly with
 L. Canto e Castro. Prior to her PHD, she published one article in an international periodical (Temido, 1999).
- Manuel Scotto (Scotto, 2001) and Patrícia de Zea Bermudez (de Zea Bermudez, 2003) worked under the supervision of Feridun Turkman. Regarding publications prior to their PhDs, I refer Scotto and Guedes Soares (2000) and de Zea Bermudez et al. (2001).
- M. João Martins (Martins MJ, 2001) worked under my co-supervision, jointly with M. Manuela Neves. Prior to her PhD, and just as happened with Teresa Alpuin, she had three articles published in international periodicals (Martins *et al.*, 1999; Gomes *et al.*, 2000; Gomes and Martins, 2001).
- Bruno Cecílio de Sousa, my MSc student, got his degree in 2002 (de Sousa, 2002), at Michigan, USA, under the joint supervision of Bruce Hill and G. Michailidis.

- M. Luísa Pereira (Pereira ML, 2002) got her degree at Universidade da Beira Interior, under the supervision of Helena Ferreira, being thus my second 'granddaughter'. Prior to her PhD, she has one article published at an international periodical (Pereira ML and Ferreira H, 2001).
- Ana Ferreira, who got her MSc degree under my supervision, got her PhD degree at Tilburg University (Ferreira A, 2002), under the joint supervision of Laurens de Haan and John Einmahl.
- I still mention the thesis by Fernanda Figueiredo (Figueiredo, 2003), under my supervision and essentially in the field of *Statistical Quality Control*, but where we can find several results in the area of *order statistics and extremes*.
- I further mention Alexandra Ramos (Ramos, 2003), who got her PhD at Surrey University, under the supervision of Anthony Ledford, and Alexandra Dias (Dias, 2003), who got her PhD at ETH, Zurich, under the supervision of Paul Embrechts. Alexandra Dias had a publication in an international periodical prior to her PhD (Dias and Embrechts, 2003).

To the **19** aforementioned PhD thesis, in the period 1994–2003, I now also add two PhD thesis supervised by Laurens de Haan in this period (Draisma, 2001, Lin, 2002), having only counted thesis under his supervision and discussed after 1999, the year Laurens joined CEAUL. Prior to their PhDs, they have articles published at international periodicals (Draisma *et al.*, 1999; de Haan and Lin, 2001).

It is indeed sensible to refer that Laurens de Haan, one of the giants in the area of *Extremes*, and author of a highly cited PhD thesis (de Haan, 1970), which I also include in the references, has regularly visited Lisbon since 1997, and this has led to the development of joint research work with several members of CEAUL. He came to Portugal in 1999, becoming then a member of CEAUL and of PORTSEA. Despite of his relevant contributions to the field prior to 1999, we have only included part of his scientific production from 1999 onwards. On the grounds of the strong cooperation developed between Laurens and members of DEIO/FCUL, and even more generally his cooperation with members of the Portuguese statistical community, DEIO has proposed a title of ULisboa '*Doutor Honoris Causa*' to Laurens de Haan. He has accepted such a distinction and the title was awarded in 2000. And in 2013 another giant in the field, Ross Leadbetter, has honored the University of Lisbon by accepting the same distinction, since no doubt, and just has I wrote at *Info-Ciências Digital* (Gomes, 2013a), when the university honors researchers of this importance it is also honored. The group has thus two of the *ULisboa Honoris Causa Doctors*.

After 2004 and up to the end of 2018, in a period of 15 years, the growth rate decreased. Anyway, and being sure that a few PhD thesis are missing, I could count **29** additional PhD thesis in the field, most of them supervised by members of our PORTSEA:

- The fourth PhD student of Tiago de Oliveira in the field of *Extremes*, Maria de Fátima Miguéns, was working in an area quite close to the main area of Tiago de Oliveira, *Multivariate Extremes*, and with a reasonably difficult research path, defended her PhD thesis only in 2004 (Miguéns, 2004), under the supervision of M. Fátima Fontes de Sousa.
- Deyuan Li (Li, 2004) got his PhD at Erasmus Rotterdam School, under the supervision of Laurens de Haan. Prior to his PhD, I mention the publication of the article, de Haan *et al.* (2002).
- Ana Paula Martins (Martins AP, 2005) got her PhD at Universidade da Beira Interior, under the supervision of Helena Ferreira and Luísa Pereira. She is thus my first scientific 'grand-grand-daughter'. Prior to her PhD, and just as happened with Teresa Alpuim and M. João Martins, I could count three articles in relevant international periodicals, Ferreira H and Martins AP (2003), Martins AP and Ferreira H (2004a,b).
- Maria Cristina Miranda (Miranda, 2005) got her PhD at DEIO/FCUL, under my supervision, jointly with Andreia Hall.
- Ana Cristina Moreira Freitas (Freitas ACM, 2005) got her PhD at Faculdade de Ciências, Universidade do Porto, under the supervision of Margarida Brito. She also published prior to her PhD (Brito and Freitas ACM, 2003).
- Frederico Caeiro (Caeiro, 2006) got his PhD at DEIO/FCUL, under my supervision. He has been co-author of five relevant articles prior to his PhD (Caeiro and Gomes, 2002a,b; Caeiro *et al.*, 2005; Gomes and Caeiro, 2002; Gomes *et al.*, 2004a). Frederico has thus beaten the record of Teresa Alpuim, M. João Martins and Ana Paula Martins, with five articles published in international periodicals prior to his PhD.
- Cláudia Neves (Neves, 2006), currently working at University of Reading, UK, and my third 'grand-daughter', got her PhD at DEIO/FCUL, under the supervision of Isabel Fraga Alves and Laurens de Haan. Se has co-authored two relevant articles prior to her PhD (Neves and Fraga Alves, 2004; Neves *et al.*, 2006).
- Sandra Dias (Dias, 2007) and Marta Ferreira (Ferreira M, 2008) got their PhD at DEIO/FCUL, under the supervision of Luísa Canto e Castro. I have thus got two additional 'grand-daughters', who fortunately had their jobs already in Portugal, and no need to go abroad.
- Under the joint supervision of Laurens de Haan and Casper de Vries, I mention Chen Zhou's PhD thesis (Zhou, 2008a). Prior to his PhD, I could count one article in a high quality journal (de Vries and Zhou, 2006).

- Dora Prata Gomes (Prata Gomes, 2008) got her PhD at Departamento de Matemática, Faculdade de Ciências e Tecnologia, UNL, under the supervision of Manuela Neves and Tiago Mexia.
- Miguel De Carvalho (De Carvalho, 2009), currently working at University of Edinburgh, UK, got his PhD at Faculdade de Ciências e Tecnologia, UNL, under the supervision of J. Tiago Mexia and Manuel Esquível.
- Lígia Henriques-Rodrigues (Henriques-Rodrigues, 2009), who was working at IME, San Paulo, Brazil, by the mid of 2018, the time I began writing this historical preprint, is now working at University of Évora, and has got her Ph.D. at DEIO/FCUL, under my supervision. Prior to her PhD, I could find Gomes and Henriques-Rodrigues (2008).
- Clara Cordeiro (Cordeiro, 2011) got her PhD at ISA, UTL, under the supervision of M. Manuela Neves. The thesis is slight away from EVT, but she has now been working in the subject. However, two of her papers prior to PhD (Cordeiro and Neves, 2009, 2010) appear to be of high relevance to the field of *Extremes*.
- Clara Viseu (Viseu, 2011), who was my MSc student, got her PhD at Universidade da Beira Interior, under the supervision of Helena Ferreira and Luísa Pereira, being thus my second 'grand-grand-daughter'. Prior to her PhD, I could count a book chapter and two articles in international periodicals (Gomes et al., 2007b, 2008d,e), in a sub-field of Extremes, slight out of the framework of her PhD and closer to her MSc thesis.
- Paulo Araújo Santos (Araújo Santos, 2011), another 'grand-son', got his degree in DEIO/FCUL, under the supervision of Isabel Fraga Alves. Prior to his PhD, I could find two articles in periodicals (Araújo Santos *et al.*, 2006; Gomes *et al.*, 2008a).
- Paula Reis (Reis, 2012) got her PhD at DEIO/FCUL, under the supervision of Luísa Canto e Castro and José António Caldeira Duarte. I have thus got another 'grand-daughter'. The article, Reis and Canto e Castro (2009), was published prior to her PhD.
- Hale Aytaç (Aytaç, 2013) got his PhD at Faculdade de Ciências da Universidade do Porto (FCUP), under the supervision of Jorge Milhazes Freitas, a colleague from FCUP, who got his Ph.D thesis in the area of Dynamical Systems, in 2006, but enthusiastically joined the group of Extremes around 2005. I indeed recall his enthusiasm about the extremal index in the Workshop on Risk Analysis and Extreme Values, at Laboratoire de Statistique Appliquée, in Paris, June, 2005, when he was only an accompanying person.

- Jointly with John Einmahl, Laurens de Haan also supervised the PhD thesis of Juan-Juan Cai (Cai, 2012), at Tilburg University. Juan-Juan has an article prior to her PhD (Cai *et al.*, 2011).
- Cecília Fonseca (Fonseca, 2013) and João Renato Sebastião (Sebastião, 2013) got their PhD at Universidade da Beira Interior, under the joint supervision of Luísa Pereira and Ana Paula Martins. They can thus be considered as my first 'grand-grand-grand' daughter and son. João Sebastião had one article prior to his PhD (Sebastião et al., 2010).
- Paula Pereira (Pereira P, 2014) got her PhD at DEIO/FCUL, under the supervision of Feridun Turkman. Two of her articles (Turkman *et al.*, 2010; Pereira P *et al.*, 2013) have been published prior to her PhD.
- Laura Cavalcante (Cavalcante, 2014) got her PhD at Universidade do Porto, under the joint supervision of Ana Cristina Moreira Freitas and Margarida Brito.
- Délia Gouveia Reis (Gouveia Reis, 2014) got her PhD at Universidade da Madeira, under the joint supervision of Luiz Carlos Guerreiro Lopes and Sandra Mendonça.
- Eduardo Sousa Costa (Sousa Costa, 2015), got the degree in 2015, at IST, Universidade de Lisboa, under the co-supervision of António Gonçalves Henriques and Anabela Leitão. I was one of the members of the 'Accompanying Committee'.
- Helena Penalva (Penalva, 2017) got her PhD at ISA/ULisboa, under my cosupervision, jointly with M. Manuela Neves and Sandra Nunes. Prior to her PhD, she published two papers in international periodicals (Penalva *et al.*, 2013, 2016).
- Andrêssa Lima de Souza (Lima de Souza, 2017) got her PhD at Universidade Federal da Bahia, under the supervision of Jorge Milhazes Freitas.
- Artur Tiago Silva (Silva AT, 2017) got a PhD at Civil Engineering, IST, ULisboa, under the supervision of Manuela Portela and Mauro Naghettini. The applied research conducted in this PhD thesis enabled the publication of four relevant articles (Silva AT and Portela, 2012; Silva AT *et al.*, 2012, 2014, 2016).
- Soraia Pereira (Pereira S, 2018) got her PhD at DEIO/FCUL, under the supervision of Feridun Turkman. Her PhD is a bit aside from the field of *Extremes*, but, apart from a paper published prior to her PhD (Soraia *et al.*, 2018), she began recently working hard in the field as can be attested by the recent ArXiv preprints, Amaral Turkman *et al.* (2020), De Carvalho M *et al.* (2020), Pereira S *et al.* (2020).

Indeed, on the basis of a nucleon formed by some of the aforementioned Doctors, the research group in the area of *Extremes* has increased at a high rate and in a healthy way, I think. Including mine and Kamil Feridun Turkman PhD thesis, I had counted up to the end of 2003 (Gomes, 2005), **28** PhD thesis in the area (**13** of them in the period 1999-2003, with the high rate of **2.6** PhD thesis per year), written by Portuguese researchers, doing now research necessarily no longer in the field of *Extremes*. Including now Laurens de Haan thesis and the 2 PhD thesis supervised by him in 2001, 2002, I could count **31** PhD thesis in the area and in that same period (**15** of them in the period 1999-2003, with the high rate of **3** PhD thesis per year). And such a rate has increased to **3.4** in the 5-years periods ending at 2005. There was then a decrease in such a rate, with around to **1.6**/per year in the 5-years periods ending at 2010 and up to 2018. But as 'a picture is worth a thousand words', I present Figure 4.

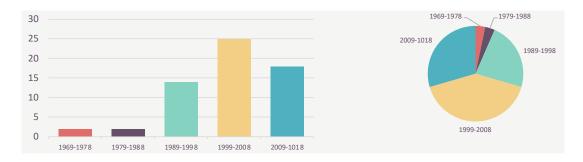


Figure 4: Number of PHD's (left) and percentages (right), along ten-years' periods

The number of Habilitation Degrees has not been as high as expected. Apart from the **5** initial members of the group, I could count only **11** additional people with an *Habilitation Degree* (Teresa Alpuim, 2002; Manuela Neves, 2003; Isabel Fraga Alves, 2003; Helena Ferreira, 2004; Manuel Scotto, 2012; Luisa Pereira, 2008; Jorge Milhazes de Freitas; 2014; Ana Cristina Moreira Freitas, 2014; Fátima Brilhante, 2015; Ana Ferreira, 2016; Miguel De Carvalho, 2018). But I may be forgetting somebody and I believe that a few members of the PORTSEA will soon apply for such a degree.

4 Conferences' organization under PORTSEA umbrella

After the organization of the 1983 NATO ASI on SEA, Feridun Turkman (jointly with Vic Barnett, University of Sheffield) organized in 1993, a SPRUCE meeting on *Statistics for the Environment*, in Lisbon, where *Extremes* played a very important role (see Barnett and Turkman, Eds., 1993). Other SPRUCE meetings have been co-

organized by Feridun, out of Portugal. But we can say that after a wide interregnum of about 15 years, these last two decades have been fruitful in the organization of international conferences in Portugal in the area of *Extremes*, with the inclusion of the area of *Risk Analysis*, where tails are also quite relevant. The **5** organizations referred to in Gomes (2007) are now **14**, as follows:

- Workshop on Statistical Modelling—Extreme Values and Additive Laws, Estoril, October 2–7, 1999. This workshop run under the sponsorship of CEAUL and the Foundation for the Science and Technology (FCT) project 'MODEST—Statistical Modeling', a project developed in the interaction of two sub-projects: the subproject 'MECAES—Stochastic Models in Environment, Ecology and Health Sciences', leaded by Kamil Feridun Turkman, and the subproject 'VELA—Extreme Values and Additive Laws', leaded by M. Ivette Gomes (1997-2000). For details, on all accepted conference papers, see Gomes et al., Eds. (1999).
- 2. Workshop on Extreme Values and Resampling Techniques, Coimbra, November 1–3, 2002. This was the first international workshop running under the sponsorship of the project 'VEXTRA—Extreme Values and Resampling Techniques', POCTI, FCT (2000-2003), and also CEAUL (see Temido and Ferreira, Eds., 2002).
- 3. Workshop on Extremes, Risk and Resampling Techniques, November 20–23, Tomar, November 20–23, 2003. This was the final international workshop running under VEXTRA's project (see Gomes, et al., Eds., 2003).
- 4. EVA 2004: Third International Symposium on Extreme Value Analysis: Theory and Practice, Aveiro, July 19–23, 2004. After Gothenburg (1998) and Leuven (2001), the III Conference on Extreme Value Analysis was held in Portugal, in a certain sense as as a recognition for what we already had done in the field (see Hall et al., Eds., 2004a).
- 5. Extremes Day in Honor of Laurens de Haan: Extremes, Risk, Safety and the Environment, Lisboa, FCUL, February 22, 2006. In 2004, Isabel Fraga Alves and I put forward a proposal for the award of a Gulbenkian Professorship (naturally granted) to Laurens. Under this Gulbenkian Professorship, Laurens de Haan had a temporary job of visiting professor at FCUL (DEIO), from the 1st of January until the 31st of December 2005. And on the occasion of his Gulbenkian Lecture, entitled 'On Extreme Value Theory or How to learn from almost Disastrous Events', under the sponsorship of CEAUL and the ERSE—Extremes, Risk, Safety and the Environment project, POCI/MAT 58876/2004 (2005–2008), we have organized this successful workshop, where we tried detecting the new advances in the main topics of ERSE project (see Fraga Alves and Gomes, Eds., 2006).

- SEER 2007: Statistical Extremes and Environmental Risk, Lisboa, February 15–17, 2007. This was the final international workshop running under ERSE's project (see Fraga Alves *et al.*, Eds., 2007b).
- 7. ISI 2007: 56th Session of the International Statistical Institute. This large event, with more than 2000 participants, was held in Lisbon, Portugal, 22-29 August. I was the Chair of the Local Program Committee and member of the International Program and National Organizing Committees. There was a strong co-operation between CEAUL and INE, the National Statistical Institute, with a high recognition of the field of Extremes (see Gomes et al., Eds., 2007c, 2008f). Such a recognition led to an invited volume of Revstat—Statistical Journal (Volume 6:1, 2008), edited by Jan Beirlant, Isabel Fraga Alves and Ross Leadbetter (Beirlant et al., Eds., 2008).
- 8. Workshop on Risk and Extreme Values in Insurance and Finance, Lisboa, June 6-7, 2011. This conference represented a unique event which brought together in Portugal the three authors of the book Modelling Extremal Events for Insurance and Finance Paul Embrechts (Zurich, Switzerland), Claudia Klüppelberg (München, Germany), and Thomas Mikosch (Copenhagen, Denmark). This international workshop run under the sponsorship of CEAUL and the project 'EXTREMA: Extremes in Today's World', PTDC/MAT/101736/2008 (2010-2013), under the leadership of M. Ivette Gomes, and the project 'Extremes in Space', PTDC/MAT/112770/2009 (2011-2013), under the leadership of Laurens de Haan (see Fraga Alves et al., Eds., 2011).
- 9. Workshop on Multivariate and Spatial Extremes: WMSE 2011, Universidade da Beira Interior (UBI), Covilhã, October 13–14, 2011. The Workshop was organized jointly by the Center of Mathematics (CMUBI) and the FCT research project Structure of Random Fields (PTDC/MAT/108575/2008), under the leadership of Luísa Pereira.
- Symposium on Recent Advances in Extreme Value Theory honoring Ross Leadbetter, Lisboa, March 18–20, 2013. This Symposium, held around the day Ross Leadbetter has been awarded a 'Honoris Causa' degree by the University of Lisbon, was organized by CEAUL, jointly with the FCT research projects Extremes in Space, PTDC/MAT/112770/2009, and Statistical Methods in Environmental and Epidemiological Processes, PTDC/MAT/118335/2010, and Strategic Project CEAUL: PEst-OE/MAT/UI0006/2011 (see Turkman et al., Eds., 2013).
- 5th International Conference on Risk Assessment (ICRA5), May 29–31, June
 Tomar, 2013. After 4 meetings organized by the International Statistical Institute-Committee on Risk Analysis (ISI-CRA), organized in Athens, San-

torini, Porto Heli and Limassol, ICRA5 was organized as part of the *Celebrations of the International Year of Statistics* and was held at the '*Instituto Politécnico de Tomar*' (IPT). This meeting was organized in honour of Lutz Edler, under the umbrella of CEAUL, UAb—Universidade Aberta, IPT and EXTREMA FCT project (see Oliveira T *et al.*, Eds., 2013), and gave rise to an invited volume of *Revstat—Statistical Journal* (Volume 14:2, 2016), edited by Christos Kitsos, Teresa Oliveira and Milan Stehlík (Kitsos *et al.*, Eds., 2016).

- 12. EVT—*Extremes in Vimeiro Today*, Vimeiro, September 8–11, 2013. This international conference was organized by Antónia Amaral-Turkman, Isabel Fraga Alves and Manuela Neves (see Fraga Alves and Neves, Eds., 2013), on the occasion of my 65th birthday and for the celebration of the 30 years of the NATO ASI on SEA, in 1983.
- 13. Satellite Meeting ISI-CRA, in honour of Professor David Banks, jointly with 10th Workshop on Statistics, Mathematics and Computation, Lisboa, July 10 and Portalegre, July 11-12, 2017 (see Oliveira T et al., Eds., 2017).
- 14. The Workshop on New Frontiers in Statistics of Extremes was organized by Patrícia de Zea Bermudez and Miguel de Carvalho, under the sponsorship of CEAUL and the Research Project, Data Fusion and Calibration Methods for Spatial Risk Analysis (PTDC/MAT-STA-28649/2017), from FCT (see Program and Book of Abstracts at https://workshopnfsextremes2020. weebly.com/uploads/1/0/1/7/101754332/book_of_abstracts.pdf).

Among the aforementioned organizations and to make a comparison with SEA 2013, I would like to further say a few words about EVT 2013 (*Extremes in Vimeiro Today*), organized by my colleagues and great friends, Antónia Amaral Turkman, Isabel Fraga Alves and Manuela Neves, to commemorate the thirty years of the Vimeiro meeting in 1983.

This was indeed another of the great PORTSEA milestones.



Figure 5: Photo of participants of EVT 2013 (Extremes in Vineiro Today)

- Of the 40 participants in SEA 1983, only around 30% were young, and only ten (25%) were women, seven of whom became (or were) PhD students in Portugal.
- And of the 81 participants in EVT 2013, more than 50% were women, and more than 40% were young people, something that I saw as very promising for the future of the area ...

And among the aforementioned conferences, I must also further say that I was very impressed by:

- EVA 2004, in which the 'extremists' and PORTSEA members Andreia Hall and Manuel Scotto played a very important role.
- ICRA5, where I highlight the relevant role of Teresa Oliveira, currently 'Chair' of ISI-CRA, and who I also consider a member of PORTSEA.
- Finally, the last international conference held in Portugal in the area, the WNFSE 2020, organized by the '*extremists*' Patrícia de Zea Bermudez and Miguel de Carvalho, current President of SPE, was held by the end of February 2020, in Lisbon, just before we went into confinement, due to COVID-19, and left me extremely satisfied and grateful, seeing that PORTSEA is still very much alive, and with the very active collaboration of several researchers from Banco de Portugal who can have a strong effect in the development of PORTSEA.

Internationally, I refer only to the following:

- All EVA conferences, organized since 1998, have had members of our PORT-SEA in their Scientific Committees. And the same happens with EVA 2021, which will take place virtually in Edinburgh, UK, next June/July, and which will further have two members of PORTSEA, Miguel de Carvalho and Cláudia Neves, in the Organizing Committee.
- KLIMATEXT—International Conference on Precipitation Extremes in a Changing Climate, Technical University of Liberec, Hejnice, Czech Republic, September 24-26, 2013. This conference run under the umbrella of CZ.1.07./2.3.00/20.0086, 'Strengthening International Cooperation of the Klimatext Research Team' (EU Project: EU structural funds through the Czeck ministry of Education, 2012–2014), with Jan Picek as co-ordinator, and M. Ivette Gomes as an international expert.
- The 'Centre International de Rencontres Mathématiques' (CIRM) International Conference on Extreme Value Theory and Laws of Rare Events, which took place in July 14-18, 2014, Marseille, France, had two other members of PORTSEA in the Organizing Committee, both from the University of Porto,

Ana Cristina Moreira Freitas and Jorge Milhazes Freitas, Corresponding Member of ACL since January 2020, and considered by many, and also by me, one of the founders of *Extremes in Dynamical Systems*.

— The 7th International Conference on Risk Analysis (ICRA7), which took place in Chicago, in May 2017, had Teresa Oliveira in the Executive Committee. ICRA7 was held in my honour, and as Risk Analysis is not my main research topic, this international tribute had a special flavour, as it seemed more like a global recognition of my contribution to Probability and Statistics.

5 The 'heart' of PORTSEA

I consider that the excellence of the PhD students that we have had is actually what has contributed the most to the internationalization of the '*Escola de Extremos*' in Portugal. But I cannot fail to mention the importance of the co-orientation of a great diversity of foreign graduate students, from different Universities: Charles University Prague, Fudan University of Shanghai, KULeuven, Pierre-et-Marie-Curie, Siegen, among others. Over the years, and the increasing number of publications, collaboration with researchers from other countries has increased significantly, as can be seen in Figure 6. We there represent **65** universities to which belong co-authors of PORTSEA members, in articles published in high-profile scientific journals.



Figure 6: Universities around the world with co-authors of members of PORTSEA

The involvement of various members of PORTSEA as Editors of scientific journals is another source of satisfaction. Among the wide range of international periodicals where members of PORTSEA have played an important role, I would like to highlight only:

- The fact that three of these members, Ana Ferreira, Laurens de Haan and myself, are in the body of Associate Editors of *Extremes*, the most prestigious journal in the area, edited by Springer, with Thomas Mikosh as current Editorin-Chief (since 2015), following Holger Rootzén (1998–2006) and Jürg Hüsler (2007–2014).
- And the fact that I was Editor-in-Chief of *Revstat-Statistical Journal*, from 2003 until the end of 2018 (a position currently held by another member of PORTSEA, Isabel Fraga Alves), having managed to place this periodical, edited by *Instituto Nacional de Estatística* (INE), with whom we have had high collaboration, among the prestigious journals of *Statistics*, with an impact factor in ISI *Web of Knowledge* since 2007.

Again thinking only on the aforementioned periodicals, *Extremes* and *Revstat*, I would like to mention the following numbers:

- I could find 42 articles co-authored by members of PORTSEA, published at *Extremes* (Beirlant et al., 2016; Caeiro and Gomes, 2006; Caeiro et al., 2016a; Cai et al., 2013, 2020; Canto e Castro and Dias, 2011; Dietrich et al., 2002; Draisma et al., 1999; Drees et al., 2018; Einmahl et al., 2013; Ferreira A and Huang, 2018; Ferreira H, 2000; Ferreira M and Canto e Castro, 2008; Fraga Alves, 2001a; Fraga Alves and De Carvalho, 2015; Fraga Alves et al., 2009, 2017; Gomes and de Haan, 1999; Gomes and Henriques-Rodrigues, 2008; Gomes and Martins, 2002; Gomes and Oliveira, 2001; Gomes et al., 2000, 2002, 2008b, 2012; de Haan, 2006; de Haan et al., 2009, 2015; Hall, 2001, 2003; Hall et al., 2004b; Leng et al., 2019; Pereira ML et al., 2017; Ramos and Ledford, 2005; Turkman et al., 2010; Valente de Freitas and Hüsler, 2003; Veltohen et al., 2019; de Vries and Zhou, 2006; de Zea Bermudez et al., 2001; Zhou, 2008b, 2017, 2018).
- Regarding Revstat, I mention the edition of volume 6:1 (Beirlant et al., 2012) and 14:2 (Kitsos et al., 2016), as well as the co-authorship of 39 articles (Araújo Santos et al., 2006; Beirlant et al., 2012; Brilhante, 2004; Brilhante et al., 2019; Caeiro and Gomes, 2008; Caeiro et al., 2005; Caetano et al., 2019; Cordeiro and Neves, 2009; De Carvalho and Ramos, 2012; Ferreira H, 2006a; Ferreira H and Ferreira M, 2020; Ferreira H and Martins AP, 2003; Ferreira M, 2010, 2013c, 2018; Ferreira M et al., 2012; Figueiredo and Gomes, 2013; Figueiredo et al., 2017; Fraga Alves et al., 2007a; Gomes et al., 2007a, 2016b; de Haan and Zhou, 2008; Hall and Scotto, 2006, 2008; Henriques-Rodrigues and Gomes, 2009; Henriques-Rodrigues et al., 2011, 2014; Neves and Fraga Alves, 2008; Oliveira A et al., 2016; Oliveira O et al., 2006; Penalva et al., 2016, 2019, 2020a; Pereira ML, 2004; Pereira S et al., 2018; Reis and Canto e Castro, 2009; Scotto, 2007; Silva I and Silva ME, 2009; Turkman, 2014).

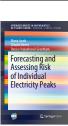
The PORTSEA has nowadays several internationally renowned names. I counted more than **60** PhD theses in the area or in very close areas, written by Portuguese researchers, and associated with degrees obtained in Portugal and abroad. But, just as I mentioned before, the number of Habilitation Degrees needs to increase. The current number of PhD and Master students in the area, although not as high as a decade ago, still promises to expand the group in the near future. However, such a number is becoming smaller, being thus more difficult to widen the group in the near future, unless our policy is slightly changed. But I think it is pertinent to refer two current PhD students in the field and in Lisbon, whom I got to know well, Ivanilda Cabral and Jessica Lomba. Ivanilda is an Assistant at Departamento de Ciência e Tecnologia da Universidade de Cabo Verde, and has been working for PhD at UNL, under the co-supervision of Frederico Caeiro and I. Ivette Gomes. Prior to the discussion of her PhD, I refer the publication of a book chapter (Caeiro et al., 2018) and two articles in international periodicals (Cabral et al., 2020a,b). Jessica Lomba, an Assistant at UNL, Nova School of Business and Economics: Lisboa, has been working for PhD, at DEIO, under the supervision of Isabel Fraga Alves. Apart from several academic merit scolarships, she has received SPE Award 2019, a research incentive award for young researchers under 35, with original and quality work, and has already a publication at a highly reputed international periodical (Lomba and Fraga Alves, 2020).

The dynamic of publication has been quite high, clearly above international average standards, with more than five hundred articles published in prestigious international journals. I limit myself to refer to the 87 articles published in the last ten years (2011-2020), co-authored by only 3 of the members of PORTSEA, two of the three pioneers in the area (in view of the death of Tiago de Oliveira in 1992), and Laurens de Haan, a member of PORTSEA, still active, and 'ULisboa Doctor Honoris Causa' (Amaral-Turkman et al., 2011; Beirlant et al., 2012, 2016; Brilhante et al., 2011, 2012, 2013a,b,c, 2014, 2019; Cabral et al., 2020; Caeiro and Gomes, 2011a,b,c, 2013, 2015a,b; Caeiro et al., 2014, 2016a,b, 2020; Cai et al., 2011, 2013, 2014; Da Camara et al., 2014; De Carvalho et al., 2013; Drees and de Haan, 2015; Drees et al., 2018; Einmahl et al., 2013, 2016, 2019; Ferreira A and de Haan, 2014, 2015; Ferreira A et al., 2012; Ferreira M et al., 2012; Figueiredo and Gomes, 2013, 2016; Figueiredo et al., 2012, 2017; Fougères et al., 2015; Gomes, 2020; Gomes and Guillou, 2015; Gomes and Henriques-Rodrigues, 2016, 2017; Gomes and Neves, 2011; Gomes and Pestana, 2011; Gomes et al., 2011a,b,c, 2012, 2013a,b,d,e, 2015a,b, 2016a,b, 2020a,b; de Haan, 2015; de Haan and Zhou, 2011; de Haan et al., 2013, 2015, 2016; Henriques-Rodrigues and Gomes, 2018; Henriques-Rodrigues et al., 2011, 2014, 2015; Leiva et al., 2016, 2019; Neves C et al., 2011; Neves MM et al., 2015; Nunes et al., 2019; Pekalp et al., 2019; Penalva et al., 2020a,b; Pereira JMC et al., 2015, 2019; Pereira P et al., 2013; Pereira S et al., 2018; Pinto et al., 2018; Reis et al., 2015; Sousa et al., 2016; Turkman, 2014; Turkman et al., 2014a; Ursu and Turkman, 2012), not all in the *Extremes and Risk Assessment* area, but in very close areas involving statistical EVT.

It should also be noted that our *School of Extremes*, despite the high contribution at the international level, has not neglected publication at the national level. This contribution can be attested to by the publication of articles in Portuguese, in the different text collections associated with SPE Congresses and edited by SPE since 1992, where the production in the area of *Extremes* has been, on average, 17% per volume.

I cannot also fail to mention five relevant books, with PORTSEA members among the co-authors:





A generic book by Laurens de Haan and Ana Ferreira (de Haan and Ferreira, 2006), with more than 2500 citations, and published by Springer, which once again attest to the invaluable contribution of Laurens de Haan to the establishment of PORTSEA;

A book in Portuguese (Gomes *et al.*, 2013c), coauthored by Ivette Gomes, Isabel Fraga Alves and Cláudia Neves, also generic, edited by SPE/INE and associated with a short course taught prior to the XXI Annual Congress of SPE, held in Aveiro;

A book on *Extremes of Nonlinear Time Series* (Turkman *et al.*, 2014b), co-authored by Feridun Turkman, Manuel Scotto and Patrícia de Zea Bermudez, edited by Springer;

Another one about *Extremes in Dynamic Systems* (Lucarini *et al.*, 2016), edited by Wiley, in which Ana Cristina Moreira Freitas and Jorge Milhazes Freitas are co-authors;

And a last one about *Risk Assessment and Extremes* (Jacob *et al.*, 2020), edited by Springer, in which Cláudia Neves is co-author.

The fields of EVT, in which PORTSEA's contribution has been important, are very diverse. In addition to a vast group with innovative work in the area of Parametric, Semi-parametric and Non-parametric Estimation of parameters of extreme events, PORTSEA has strong groups in the areas of

- $-\,$ Statistical Choice of Extremal Models,
- Extremes and Risk Modelling,

- Environmental Extremes,
- Extremes of Dynamical Systems,
- Extremes of Dependent Sequences, and
- Spatial Extremes.

And, as a prediction, I hope that we shall soon have a group of

- Extremes in Genetics and another in
- Extremes in Epidemic Situations.

In view of the results obtained, I am led to believe that our '*Escola de Extremos*' (or our PORTSEA) has in fact achieved a healthy growth in the area. The dynamism of the Group has allowed a high international recognition of the School of Extremes in Portugal, a country of '*nice extremists*' at one end of Europe.

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References

- ALPUIM MT (1986). Record values in populations with increasing or random dimension. Metron 43:3-4, 145–155.
- [2] ALPUIM MT (1988). High level exceedences in stationary sequences with extremal index. Stochastic Processes and their Applications 30, 1–16.
- [3] ALPUIM MT (1989). Contribuições à Teoria de Extremos em Sucessões Dependentes. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [4] ALPUIM MT and ATHAYDE E (1990). On the stationary distribution of some extremal markovian sequences. J. Appl. Probab. 27, 291-302.
- [5] AMARAL-TURKMAN MA, TURKMAN KF, LE PAGE Y and PEREIRA JMC (2011). Hierarchical space-time models for fire ignition and percentage of land burned by wildfires. *Envir.* and Ecol. Statistics 18, 601–617.
- [6] AMARAL TURKMAN MA, TURKMAN KF, ZEA BERMUDEZ P DE, PEREIRA S, PEREIRA P and DE CARVALHO M. (2020). *Calibration methods for spatial Data*. ArXiv:2009.13629.
- [7] ARAÚJO SANTOS P (2011). Excesses, Durations and Forecasting Value-at-Risk. Tese de Doutoramento, DEIO, Faculdade de Ciências da Universidade de Lisboa.
- [8] ARAÚJO SANTOS P, FRAGA ALVES MI and GOMES MI (2006). Peaks over random threshold methodology for tail index and quantile estimation. *Revstat—Statist. J.* 4:3, 227–247.
- [9] ATHAYDE ME (1994). Estudo de Algumas Sucessões Markovianas com Relevo para a Teoria de Extremos. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [10] ATHAYDE ME and GOMES MI (1987). Multivariate extremal models under non-classical situations. In P. Bauer et al. (eds.), Mathematical Statistics and Probability Theory, Vol. B, 1–9, D. Reidel, Dordrecht.
- [11] AYTAÇ H (2013). Extreme Values and Recurrence for Deterministic and Stochastic Dynamics. Tese de Doutoramento, Faculdade de Ciências, Universidade do Porto.
- [12] BARÃO MI (1993). Comparação de Populações de Gumbel. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.

- [13] BARNETT V and TURKMAN KF, Eds. (1993). Statistics for the Environment. J. Wiley & Sons, Chichester/New York/Brisbane/Toronto/Singapore.
- [14] BEIRLANT J, FRAGA ALVES MI and LEADBETTER R, Eds. (2008). Special Issue on 'Collection of Surveys on Tail Event Modeling', *Revstat—Statistical Journal* 6:1, Instituto Nacional de Estatística.
- [15] BEIRLANT J, CAEIRO F and GOMES MI (2012). An overview and open research topics in the field of statistics of univariate extremes. *Revstat—Statist. J.* 10:1, 1–31
- [16] BEIRLANT J, FRAGA ALVES MI and GOMES MI (2016). Tail fitting for truncated and non-truncated Pareto-type distributions. *Extremes* 19:3, 429–462.
- [17] BRILHANTE MF (1999). Inferência Estatística em Modelos Não-Gaussianos com Recurso a Spacings e Outras Funções de Estatísticas Ordinais. Tese de Doutoramento, Universidade dos Açores.
- [18] BRILHANTE MF (2004). Exponential versus generalized Pareto a resistant and robust test. *Revstat—Statist. J.* 2:1, 1–13.
- [19] BRILHANTE MF, GOMES MI and PESTANA DD (2011). BetaBoop brings in chaos. Chaotic Modelling and Simulation (CMSIM) 1, 39–50.
- [20] BRILHANTE MF, GOMES MI and PESTANA DD (2012). Extensions of Verhulst model in population dynamics and extremes. *Chaotic Modeling and Simulation* (CMSIM) 2:4, 575– 591.
- [21] BRILHANTE MF, GOMES MI and PESTANA DD (2013a). A simple generalization of the Hill estimator. *Computational Statistics and Data Analysis* **57**:1, 518-535.
- [22] BRILHANTE MF, GOMES MI and PESTANA DD (2013b). Multifractals tied to extensions of Panjer's iterative procedures. *Chaotic Modeling and Simulation* (CMSIM) 3:1, 39–50.
- [23] BRILHANTE MF, GOMES MI and PESTANA DD (2013c). Panjer randomized Fibonacci model and dynamic instabilities in population growth models. *Chaotic Modeling and Simulation* (CMSIM) 3:4, 495-509.
- [24] BRILHANTE MF, GOMES MI and PESTANA DD (2014). Extensions of the Verhulst model, order statistics and products of independent uniform random variables. *Chaotic Modeling* and Simulation (CMSIM) 4:4, 315-322.
- [25] BRILHANTE MF, GOMES MI and PESTANA DD (2019). Modelling risk of extreme events in generalized Verhulst models. *Revstat—Statist. J.* 17:2, 145–162.
- [26] BRITO M (1986). Sur l'encadrement optimal presque sûr dans un échantillon ordonné. C.R. Acad. Sci. Paris, Série I: Math. 303:16, 821–824.
- [27] BRITO M (1987). Encadrement Presque Sûr des Statistiques d'Ordre. Doctoract d'État, Université de Paris VI.
- [28] BRITO M and FREITAS ACM (2003). Limiting behaviour of a geometric-type estimator for tail indices. *Insurance: Mathematics and Economics* **33**, 211–216.
- [29] CABRAL I, CAEIRO F and GOMES MI (2020). On the comparison of several classical estimators of the extreme value index. *Communications in Statistics—Theory and Methods*. On-line: April 4, 2020. DOI: 10.1080/03610926.2020.1746970.
- [30] CAEIRO F (2006). Estimação de Parâmetros de Acontecimentos Raros. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [31] CAEIRO F and GOMES MI (2002a). A class of "asymptotically unbiased" semi-parametric estimators of the tail index. *Test* **11**:2, 345–364.
- [32] CAEIRO F and GOMES MI (2002b). Bias reduction in the estimation of parameters of rare events. Theory of Stochatic Processes 8 (24), 1-2, 67–76.
- [33] CAEIRO F and GOMES MI (2006). A new class of estimators of a 'scale' second order parameter. *Extremes* 9, 193–211.

- [34] CAEIRO F and GOMES MI (2008). Minimum-variance reduced-bias tail index and high quantile estimation. *Revstat—Statist. J.* **6**:1, 1–20-
- [35] CAEIRO F and GOMES MI (2011a). Asymptotic comparison at optimal levels of reduced-bias extreme value index estimators. *Statistica Neerlandica* **65**:4, 462–488.
- [36] CAEIRO F and GOMES MI (2011b). Computational validation of an adaptive choice of optimal sample fractions. Bull. Internat. Statist. Inst. LXIV (Electronic publication, 8 pages). Available at: http://2011.isiproceedings.org/papers/450077.pdf
- [37] CAEIRO F and GOMES MI (2011c). Semi-parametric tail inference through probabilityweighted moments. J. Statistical Planning and Inference 141:2, 937—950.
- [38] CAEIRO F and GOMES MI (2013). The role of bootstrap methodologies in the estimation of a negative extreme value index. *Bull. Internat. Statist. Inst.* LXV (Electronic publication, 6 pages). Available at: http://www.statistics.gov.hk/wsc/IPS010-P3-S.pdf
- [39] CAEIRO F and GOMES MI (2015a). Bias reduction in the estimation of a shape second-order parameter of a heavy tailed model. J. Statist. Comput. and Simul. 85:17, 3405–3419.
- [40] CAEIRO F and GOMES MI (2015b). Revisiting the maximum likelihood estimation of a positive extreme value index. Journal of Statistical Theory and Practice 9:1, 200–218.
- [41] CAEIRO F, GOMES MI and PESTANA D (2005). Direct reduction of bias of the classical Hill estimator. *Revstat—Statist. J.* **3**:2, 113–136.
- [42] CAEIRO F, GOMES MI and VANDEWALLE B (2014). Semi-Parametric Probability-Weighted Moments Estimation Revisited. *Methodology and Computing in Appl. Probab.* 16:1, 1–29.
- [43] CAEIRO F, GOMES MI, BEIRLANT J and DE WET T (2016a). Mean-of-order-p reduced-bias extreme value index estimation under a third-order framework. *Extremes* **19**:4, 561–589.
- [44] CAEIRO F, GOMES MI and HENRIQUES-RODRIGUES L (2016b). A location invariant probability weighted moment estimation of the extreme value index. International Journal of Computer Mathematics 93:4, 676—695.
- [45] CAEIRO F, CABRAL I and GOMES MI (2018). Improving asymptotically unbiased extreme value index estimation. In Oliveira TA, Kitsos C, Oliveira A and Grilo LM, Eds., *Recent Studies on Risk Analysis and Statistical Modeling*, Springer, 155–163.
- [46] CAEIRO F, GOMES MI, HENRIQUES-RODRIGUES L and CABRAL I (2020). Minimumvariance reduced-bias estimation of the extreme value index: A theoretical and empirical study. *Computational and Mathematical Methods*, 2:e1101 (17 pages)
- [47] CAETANO CP and ZEA BERMUDEZ P DE (2019). Modeling large values of systolic blood pressure in the portuguese population. *Revstat—Statist. J.* 17:2, 163–186.
- [48] CAI J-J (2012). Estimation concerning Risk under Extreme Value Conditions. Tllburg University.
- [49] CAI J-J, EINMAHL JHJ and HAAN, L DE (2011). Estimation of extreme risk regions under multivariate regular variation. Annals of Statistics 39, 1803–1826.
- [50] CAI J-J, HAAN L DE and ZHOU C (2013). Bias correction in extreme value statistics with index around zero. *Extremes* 16: 2, 173–201.
- [51] CAI J-J, EINMAHL JHJ, HAAN L DE and ZHOU C (2014). Estimation of the marginal expected shortfall: the mean when a related variable is extreme. *Journal of the Royal Statistical Society, Series B* 77, 417–442.
- [52] CAI J-J, WAN P and OZEL G (2020). Parametric and non-parametric estimation of extreme earthquake event: the joint tailinference for mainshocks and aftershocks. *Extremes*, https: //doi.org/10.1007/s10687-020-00400-4
- [53] CANTO E CASTRO L (1987). Uniform rates of convergence in extreme-value theory: normal and gamma models. Ann. Sc. Univ. Clermont Ferrand II, Probab. Appl. 6, 25-41.
- [54] CANTO E CASTRO L (1992). Velocidades de Convergência em Teoria de Valores Extremos. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.

- [55] CANTO E CASTRO, L. and DIAS, S. (2011). Generalized Pickands' estimators for the tail index parameter and max-semistability. *Extremes* 14:4, 429–449.
- [56] CAVALCANTE L (2014). Extreme Values, High Order Quantiles and Applications. Tese de Doutoramento, Universidade do Porto.
- [57] CORDEIRO C (2011). Métodos de Reamostragem e Previsão em Séries Temporais. Tese de Doutoramento em Matemática, Ramo de Estatística, Instituto Superior de Agronomia, Universidade Técnica de Lisboa.
- [58] CORDEIRO C and NEVES MM (2009). Forecasting time series with Boot.EXPOS procedure. *Revstat—Statist. J.* 7:2, 135–149.
- [59] CORDEIRO C and NEVES MM (2010). Exponencial smoothing and resampling techniques in time series prediction. *Discussiones Mathematicae Probab. and Statistics* **30**:1, 87–101.
- [60] CRATO N (1992). Some Mispecification Problems in Long-memory Time Series Models. PhD Thesis, University of Delaware, USA.
- [61] DA CAMARA CC, CALADO TJ, ERMIDA SL, TRIGO IF, AMRAOUI M and TURKMAN KF (2014). Calibration of the Fire Weather Index over Mediterranean Europe based on fire activity retrieved from MSG satellite imagery. *Internat. Journal of Wildland Fire* 23:7, 945–958.
- [62] DE CARVALHO M (2009). Extremum Estimators and Stochastic Optimization Methods. Tese de Doutoramento, Departamento de Matemática, Faculdade de Ciências e Tecnologia, Universidade Nova de Lisboa.
- [63] DE CARVALHO M and RAMOS A (2012). Bivariate Extreme Statistics, II. Revstat—Statist. J. 10:1, 83–104.
- [64] DE CARVALHO M, TURKMAN KF and RUA A (2013). Dynamic threshold modelling and the US business cycle. J. Royal Statistical Society, Ser. C 62, 535–550.
- [65] DE CARVALHO M, PEREIRA S, PEREIRA P and ZEA BERMUDEZ P DE (2020). An Extreme Value Bayesian Lasso for the Conditional Bulk and Tail. ArXiv:2010.07164.
- [66] DIAS A (2003). Copula Inference for Finance and Insurance, ETH, Zurich.
- [67] DIAS A and EMBRECHTS P (2003). Change-point analysis for dependence. Insurance Mathematics and Economics 32(1), 152–152.
- [68] DIAS S (2007). Inferência Estatística em Modelos Max-semiestáveis. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [69] DIETRICH D, HAAN L DE and HUESLER J (2002). Testing extreme value conditions. Extremes 5, 71–85.
- [70] DRAISMA G (2001). Parametric and Semi-parametric Methods in Extreme Value Theory. PhD Thesis, Tinbergen Institute, University of Rotterdam.
- [71] DRAISMA G, HAAN L DE, PENG L and THEMIDO PEREIRA T (1999). A bootstrapbased method to achieve optimality in estimating the extreme value index. *Extremes* 2:4, 367–404.
- [72] DREES H AND HAAN L DE (2015). Estimating failure probabilities. Bernoulli 21:2, 957– 1001.
- [73] DREES H, HAAN L DE and TURKMAN KF (2018). Extreme value estimation for discretely sampled continuous processes. *Extremes* **21**, 533–550.
- [74] EINMAHL JHJ, HAAN L DE and KRAJINA A (2013). Estimating extreme multivariate quantile regions. *Extremes* 16, 121–146
- [75] EINMAHL JHJ, HAAN L DE and ZHOU C (2016). Statistics of heteroscedastic extremes. Journal of the Royal Statistical Society, Series B 78, 31–51.
- [76] EINMAHL JJ, EINMAHL JHJ and HAAN L DE (2019). Limits to human life span through extreme value theory. *Journal of the American Statistical Association* **114**, 111–527.
- [77] FERREIRA A (2002). Statistics of Extremes. Estimation and Optimality, PhD Thesis, Tllburg University.

- [78] FERREIRA A and HAAN L DE (2014). The generalized Pareto process; with a view towards application and simulation. *Bernoulli* **20**:4, 1717–1737.
- [79] FERREIRA A and HAAN L DE (2015). On the block maxima method in extreme value theory: PWM estimators, Ann. Statist. 43:1, 276–298.
- [80] FERREIRA A and HUANG F (2018). Is human life limited or unlimited? (A discussion of the paper by Holger Rootzén and Dmitrii Zholud). *Extremes* 21:3, 373–382.
- [81] FERREIRA A, HAAN L DE and ZHOU C (2012). Exceedance probability of the integral of a stochastic process. *Journal of Multivariate Analysis* 105:1, 241–257.
- [82] FERREIRA H (1993). Joint exceedances of high levels under a local dependence condition. J. Appl. Probab. 30, 112–120.
- [83] FERREIRA H (1994). Condições de Dependência Local em Teoria de Valores Extremos. Tese de Doutoramento, Universidade de Coimbra.
- [84] FERREIRA H (2000). A note on extremes of concomitants of order statistics. Extremes 3:4, 385–392.
- [85] FERREIRA H (2006a). A new dependence condition for time series and the extremal index of higher-order Markov chains. *Revstat-Statist. J.* 4:2, 143-151.
- [86] FERREIRA H AND FERREIRA M (2020). Dissecting the multivariate extremal index and tail dependence. *Revstat-Statist. J.* 18:4, 501–520.
- [87] FERREIRA H and MARTINS AP (2003). The extremal index of sub-sampled periodic sequences with strong local dependence. *Revstat—Statist. J.* 1, 15–24.
- [88] FERREIRA M (2008). Extremos em Séries Temporais Max-Autorregressivas. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [89] FERREIRA M (2010). Estimation of the parameter of a pARMAX model. Revstat—Statist. J. 8:2, 139–149.
- [90] FERREIRA M (2013c). Nonparametric estimation of the tail-dependence coefficient. *Revstat Statist. J.* **11**:1, 1–16.
- [91] FERREIRA M (2018). Heuristic tools for the estimation of the extremal index: a comparison of methods. *Revstat—Statist. J.* 16:1, 115–136.
- [92] FERREIRA M and CANTO E CASTRO L (2008). Tail and dependence behaviour of levels that persist for a fixed period of time. *Extremes* 11:2, 113–133.
- [93] FERREIRA M, GOMES MI and LEIVA V (2012). On an extreme value version of the Birnbaum-Saunders distribution. *Revstat—Statist. J.* 10:2, 181–210.
- [94] FIGUEIREDO F (2003). Controlo Estatístico da Qualidade Métodos Robustos. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [95] FIGUEIREDO F and GOMES MI (2013). The skew-normal distribution in SPC. Revstat—Statist. J. 11:1, 83–104.
- [96] FIGUEIREDO F and GOMES MI (2016). The total median statistic to monitor contaminated normal data. Quality Technology and Quantitative Management 13:1, 78–87.
- [97] FIGUEIREDO F, GOMES MI, HENRIQUES-RODRIGUES L and MIRANDA C (2012). A computational study of a quasi-PORT methodology for VaR based on second-order reduced-bias estimation. J. Statist. Comput. and Simul. 82:4, 587–602.
- [98] FIGUEIREDO F, GOMES MI and HENRIQUES-RODRIGUES L (2017). Value-at-risk estimation and the PORT mean-of-order-p methodology. *Revstat—Statist. J.* 15:2, 187–204.
- [99] FONSECA, CECÍLIA (2013). Coficientes de Dependência em Campos Aleatórios Maxestáveis. Tese de Doutoramento em Matemática Aplicada, Universidade da Beira Interior.
- [100] FOUGÈRES AL, DE HAAN L and MERCADIER C (2015). Bias correction in multivariate extremes. Annals of Statistics 43:2, 903–934.
- [101] FRAGA ALVES MI (1992a). Inferência Estatística de Modelos Extremais. Tese de Doutoramento, DEIO, Faculdade de Ciências da Universidade de Lisboa.

- [102] FRAGA ALVES MI (1992b). The influence of central observations on discrimination among multivariate extremal models. Theory of Probability and its Applications 32, 395–398.
- [103] FRAGA ALVES MI (2001a). A location invariant Hill-Type estimator. Extremes 4:3, 199–217.
- [104] FRAGA ALVES MI and DE CARVALHO M (2015). An interview with Ivette Gomes. Extremes 18:4, 563–583.
- [105] FRAGA ALVES MI and GOMES MI, Eds. (2006). Extremes Day in Honor of Laurens de Haan: Extremes, Risk, Safety and the Environment. CEAUL editions.
- [106] FRAGA ALVES MI and NEVES MM, Eds. (2013). Extremes in Vimeiro Today: Extended Abstracts. CEAUL/INE Editions, ISBN:978-989-733-023-0 (x+180 pages).
- [107] FRAGA ALVES MI, GOMES MI and HAAN L DE (2003). A new class of semi-parametric estimators of the second order parameter. *Portugaliae Mathematica* **60**:2, 193–213.
- [108] FRAGA ALVES MI, GOMES MI, HAAN L DE and NEVES C (2007a). A note on second order conditions in extreme value theory: linking general and heavy tails conditions. *Revstat—Statist. J.* 5:3, 285–305.
- [109] FRAGA ALVES MI, GOMES MI, DE HAAN L and TURKMAN KF, Eds. (2007b). Statistical Extremes and Environmental Risk. CEAUL Editions, ISBN:978-972-8859-69-5 (94 pages).
- [110] FRAGA ALVES MI, GOMES MI, HAAN L DE and NEVES C (2009). Mixed moment estimators and location invariant alternatives. *Extremes* 12, 149–185.
- [111] FRAGA ALVES MI, GOMES MI, DE HAAN L and NEVES C, Eds. (2011). Risk and Extreme Values in Insurance and Finance: Book of Abstracts. CEAUL Editions, ISBN: 978-989-8203-73-1, Depósito Legal: 325764 / 11 (x + 120 pages).
- [112] FRAGA ALVES MI, NEVES C and ROSÁRIO, P (2017). A general estimator for the right endpoint with an application to supercentenarian women's records. *Extremes* 20:1, 199–237.
- [113] FRANSÉN, A. and TIAGO DE OLIVEIRA J (1984). Statistical choice of univariate extreme models II. In Tiago de Oliveira (ed.), *Statistical Extremes and Applications*, 373–394, D. Reidel, Dordrecht.
- [114] FREITAS ACM (2005). Estimação do Coeficiente de Cauda Exponencial: Aplicação à Teoria do Risco. Tese de Doutoramento, Universidade do Porto.
- [115] FREITAS ACM and FREITAS JM (2018). An interview with Ivette Gomes, In Freitas JM. (ed.), CIM Bulletin, 36–41.
- [116] GOMES J (1996). Extreme value theory for a thermal energy storage model. Statist. Probab. Lett. 30:1, 25-31.
- [117] GOMES J and OLIVEIRA O (1997). Limit laws for a sequence between the maximum and the sum of independent exponentials. *Statist. Probab. Lett.* 35:1, 25-32.
- [118] GOMES MI (1978). Some Probabilistic and Statistical Problems in Extreme Value Theory. PhD Thesis, University of Sheffield.
- [119] GOMES MI (1979a). Extremal i-variate laws in stationary sequences. Rev. Univ. Santander 2, 1017–1019.
- [120] GOMES MI (1979b). Rates of convergence in extreme value theory. Rev. Univ. Santander 2, 1021–1023.
- [121] GOMES MI (1980a). Limit laws for the maximum values of a class of strong mixing discrete random variables. *Publ. Univ. Aut. Barcelona* 22, 139-142.
- [122] GOMES MI (1980b). On maxima of waiting times. Portugaliae Mathematica 39 (Special issue in honor of António Monteiro), 331–339.
- [123] GOMES MI (1981a). An i-dimensional limiting distribution function of largest values and its relevance to the statistical theory of extremes. In C. Taillie et al. (eds.), *Statistical Distributions in Scientific Work*, Vol. 6, 389–410 D Reidel, Dordrecht.

- [124] GOMES MI (1981b). Extremal Models in Economy. Proceedings 15th CIRET (Center for International Reservent on Economic Tendency Surveys) Conference, F1/1-23.
- [125] GOMES MI (1982). A note on statistical choice of extremal models. Actas IX Jorn. Hispano-Lusas, 653–655.
- [126] GOMES MI (1984a). Concomitants in a multidimensional extreme model. In J. Tiago de Oliveira ed., Statistical Extremes and Applications, 353-364, D. Reidel, Dordrecht.
- [127] GOMES MI (1984b). Estimation procedures in an i-dimensional extremal model. Actas XIV Reunion Soc. Espan. Inv. Oper. Estad. Inform., Vol. I, 264–274.
- [128] GOMES MI (1984c). Penultimate limiting forms in extreme value theory. Ann. Inst. Statist. Math. 36A, 71–85.
- [129] GOMES MI (1984d). Robustness of Gumbel statistic for distribution functions in the domain of attraction of a type I distribution of largest values. In T. Havránek, Z. Sidák and M. Novak (eds.) COMPSTAT 84: Proceedings in Computational Statistics, 61–66, Physica-Verlag.
- [130] GOMES MI (1984e). Statistical choice in a multivariate GEV model. Actas do III Colóquio de Estatística e Investigação Operacional, 235–244.
- [131] GOMES MI (2005). "Extremistas" num extremo da Europa. In Rosado F (ed.). Memorial da Sociedade Portuguesa de Estatística, SPE editions, 37–46.
- [132] GOMES MI (2007). Memorial da Escola. Boletim da Sociedade Portuguesa de Estatística, Primavera de 2007, SPE Editions, 37–51.
- [133] GOMES MI (2013a). Extremistas da Minha Terra. Info-Ciências Digital. Acessível em: http: //www.fc.ul.pt/pt/noticia/26-02-2013/extremistas-da-minha-terra
- [134] GOMES MI (2013b). Penultimate Approximations: Past, Present ... and Future? Preprint associated with talk at EVT 2013, Extremes in Vimeiro Today. RG preprint available at: https://www.researchgate.net/publication/333949368_PENULTIMATE_ APPROXIMATIONS_PAST_PRESENT_and_FUTURE
- [135] GOMES MI (2017). A 'Escola de Extremos' em Portugal—'Extremistas' num Extremo da Europa. Preprint associated with talk at the imposition of the degree of Emeritus Professor, ULisboa. RG preprint available at: https://www.researchgate.net/publication/ 324538105_A_Escola_de_Extremos_em_Portugal_-Extremistas_num_Extremo_da_ Europa
- [136] GOMES MI (2020). Revisiting rates of convergence and penultimate approximations for extremes. Annales Univ. Sci. Budapest., Sect. Comp. 50, 135–149.
- [137] GOMES MI and ALPUIM MT (1986). Inference in multivariate generalized extreme value models. Scandinavian J. Statistics 13, 291–300.
- [138] GOMES MI and CAEIRO F (2002). Bias reduction in the estimation of parameters of rare events. Theory of Stochatic Processes 8:24, 1-2, 67–76.
- [139] GOMES MI and GUILLOU A (2015). Extreme Value Theory and Statistics of Univariate Extremes: A Review. International Statistical Review 83:2, 263–292.
- [140] GOMES MI and DE HAAN L (1999). Approximation by penultimate extreme value distributions. Extremes 2:1, 71–85.
- [141] GOMES MI and HENRIQUES-RODRIGUES L (2008). Tail index estimation for heavy tails: accommodation of bias in the excesses over a high threshold. *Extremes* 11:3, 303–328.
- [142] GOMES MI and HENRIQUES-RODRIGUES L (2016). Competitive estimation of the extreme value index. Statist. and Probab. Letters 117, 128–135.
- [143] GOMES MI and HENRIQUES-RODRIGUES L (2017). Erratum to: Competitive estimation of the extreme value index [Statist. Probab. Lett. 117 (2016) 128–135]. Statist. and Probab. Letters 130, 40–41.
- [144] GOMES MI and MARTINS MJ (2001). Generalizations of the Hill estimator asymptotic versus finite sample behaviour. J. Statist. Planning and Inference 93, 161–180.

- [145] GOMES MI and MARTINS MJ (2002). Asymptotically unbiased' estimators of the tail index based on external estimation of the second order parameter. *Extremes* 5:1, 5–31.
- [146] GOMES MI and MONTFORT MAJ VAN (1986). Exponentiality versus Generalized Pareto, quick tests. In K. Cehak (ed.), III International Conf. on Statistical Climatology: Proceedings, Osterreichische Gesellschaft fur Meteorologie, Vienna, Austria, pp. 185–195.
- [147] GOMES MI and NEVES MM (2011). Estimation of the extreme value index for randomly censored data. *Biometrical Letters* 48:1, 1–22.
- [148] GOMES MI and OLIVEIRA O (2001). The bootstrap methodology in Statistics of Extremes — choice of the optimal sample fraction. *Extremes* 4:4, 331–358.
- [149] GOMES MI and PESTANA DD (1978). The use of fractional calculus in probability theory. Portugaliae Mathematica 37, 259–271.
- [150] GOMES MI and PESTANA DD (1981a). Nota sobre o domínio de atracção de de leis estaáveis. Actas VIII Jornadas Luso-Espanholas de Matemática, Vol. II, 339-346.
- [151] GOMES MI and PESTANA DD (1981b). On the domain of attraction of stable and of extreme value distributions. Bull. Greek Math. Soc. 22, 105-120.
- [152] GOMES MI and PESTANA DD (2011). A note on the adaptive choice of the optimal threshold in extreme value analysis. *Bull. Internat. Statist. Inst.* LXIV (Electronic publication, 8 pages). Available at: http://2011.isiproceedings.org/papers/950425.pdf
- [153] GOMES MI, PESTANA DD, CANTO E CASTRO L, FRAGA ALVES MI and MARTINS MJ, Eds. (1999). Extreme Values and Additive Laws. CEAUL editions.
- [154] GOMES MI, MARTINS MJ and NEVES MM (2000). Alternatives to a semi-parametric estimator of parameters of rare events: the Jackknife methodology. *Extremes* 3:3, 207–229.
- [155] GOMES MI, DE HAAN L and PENG L (2002). Semi-parametric estimation of the second order parameter in statistics of extremes. *Extremes* 5:4, 387–414.
- [156] GOMES MI, DE HAAN L, PESTANA D, CANTO E CASTRO L and FRAGA ALVES MI, Eds. (2003). Extremes, Risk and Resampling Techniques: Extended Abstracts. CEAUL Editions, ISBN: 972-8628-91-9 (98 pages).
- [157] GOMES MI, CAEIRO F and FIGUEIREDO F (2004a). Bias reduction of a extreme value index estimator trough an external estimation of the second order parameter. *Statistics* 38(6): 497– 510.
- [158] GOMES MI, DE HAAN L and PESTANA DD (2004b). Joint exceedances of the ARCH process. J. Applied Probab. 41:3, 919–926.
- [159] GOMES MI, DE HAAN L and PESTANA DD (2006). Correction: 'Joint exceedances of the ARCH process'. J. Applied Probab. 43:4, 1206.
- [160] GOMES MI, MARTINS MJ and NEVES MM (2007a). Improving second order reduced bias extreme value index estimation, *Revstat—Statist. J.* 5:2, 177–207.
- [161] GOMES MI, MIRANDA C and VISEU C (2007b). Reduced bias extreme value index estimation and the Jackknife methodology, *Statistica Neerlandica* 61:2, 243–270.
- [162] GOMES MI, PESTANA D and SILVA P, Eds. (2007c). ISI 2007 Book of Abstracts. CEAUL, INE and ISI editions, ISBN:978-972-8859-71-8 (lxv+689 pages).
- [163] GOMES MI, FRAGA ALVES MI and ARAÚJO SANTOS P (2008a). PORT Hill and Moment estimators for heavy-tailed models, Commun. Statist. – Simul. & Comput. 37, 1281–1306.
- [164] GOMES MI, CANTO E CASTRO L, FRAGA ALVES MI and PESTANA DD (2008b). Statistics of extremes for iid data and breakthroughs in the estimation of the extreme value index: Laurens de Haan leading contributions, *Extremes* 11:1, 3–34.
- [165] GOMES MI, DE HAAN L and HENRIQUES-RODRIGUES L (2008c). Tail Index estimation for heavy-tailed models: accommodation of bias in weighted log-excesses. J. Royal Statistical Soc. B 70:1, 31–52.

- [166] GOMES MI, HENRIQUES-RODRIGUES L, VANDEWALLE B and VISEU C (2008d). A heuristic adaptive choice of the threshold for bias-corrected Hill estimators. J. Statist. Comput. and Simulation 78:2, 133–150.
- [167] GOMES MI, PESTANA DD, HENRIQUES-RODRIGUES L and VISEU C (2008e). Tail behaviour: an empirical study. In Arnold, B.C., Balakrishnan, N., Sarabia, J.M. & Mínguez, R. (eds.), Advances in Mathematical and Statistical Modeling, Chapter 14, pp. 195-207, ISBN 978-0-8176-4625-7, Birkhauser, Boston.
- [168] GOMES MI, PINTO MARTINS JA and SILVA JA, Eds. (2008f). Bull. Internat. Statist. Inst. LXII (Electronic publication, lxii+6251 pages). International Statistical Institute (ISI) editions.
- [169] GOMES MI, HENRIQUES-RODRIGUES L and MIRANDA C (2011a). Reduced-bias locationinvariant extreme value index estimation: a simulation study. Comm. Statist.—Simul. and Comput. 40:3, 424–447.
- [170] GOMES MI, MENDONÇA S and PESTANA DD (2011b). Adaptive reduced-bias tail index and VaR estimation via the bootstrap methodology. *Comm. in Statistics – Theory and Methods* 40:16, 2946–2968.
- [171] GOMES MI, PESTANA DD and PESTANA P (2011c). Sir Pinski rides again. Chaotic Modeling and Simulation (CMSIM) 1, 77–90.
- [172] GOMES MI, FIGUEIREDO F and NEVES MM (2012). Adaptive estimation of heavy right tails: resampling-based methods in action. *Extremes* 15, 463–489.
- [173] GOMES MI, FERREIRA M and LEIVA V (2013a). The extreme value Birnbaum-Saunders model, its moments and an application in biometry. *Biometrical Letters* 49:2, 81–94.
- [174] GOMES MI, FERREIRA M and LEIVA V (2013b). The extreme value Birnbaum-Saunders model in athletics. Bull. Internat. Statist. Inst. LXV (Electronic publication, 6 pages). Available at: http://www.statistics.gov.hk/wsc/STS084-P2-S.pdf
- [175] GOMES MI, FRAGA ALVES MI and NEVES C (2013c). Análise de Valores Extremos: Uma Introdução. Edições SPE and INE, Lisboa, Portugal, ISBN: 978-972-8890-30-8 (viii+267 pages).
- [176] GOMES MI, HENRIQUES-RODRIGUES L, FRAGA ALVES MI and MANJUNATH BG (2013d). Adaptive PORT-MVRB estimation: an empirical comparison of two heuristic algorithms. J. Statist. Comput. and Simul. 83:6, 1129–1144.
- [177] GOMES MI, MARTINS MJ and NEVES MM (2013e). Generalized jakknife-based estimators for univariate extreme-value modelling. *Comm. in Statist.: Theory and Methods* 42:7, 1227– 1245.
- [178] GOMES MI, BRILHANTE MF, CAEIRO F and PESTANA DD (2015a). A new partially reduced-bias mean-of-order-p class of extreme value index estimators. *Computational Statistics and Data Analysis* 82, 223–237.
- [179] GOMES MI, FIGUEIREDO F, MARTINS MJ and NEVES MM (2015b). Resampling methodologies and reliable tail estimation. South African Statistical Journal 49, 1–20.
- [180] GOMES MI, BRILHANTE MF and PESTANA DD (2016a). New reduced-bias estimators of a positive extreme value index. Communications in Statistics: Simulation and Computation 45:3, 833–862.
- [181] GOMES MI, HENRIQUES-RODRIGUES L and MANJUNATH BG (2016b). Mean-of-order-p location-invariant extreme value index estimation. *Revstat—Statist. J.* 14:3, 273–296.
- [182] GOMES MI, CAEIRO F, FIGUEIREDO F, HENRIQUES-RODRIGUES L and PESTANA DD (2020a). Corrected Hill versus partially reduced-bias value-at-risk estimation. *Commun. in Statist.: Simul. and Comput.* 49:4, 867–875.

- [183] GOMES MI, CAEIRO F, FIGUEIREDO F, HENRIQUES-RODRIGUES L A and PESTANA DD (2020b). Reduced-bias and partially reduced-bias mean-of-order-p value-at-risk estimation: a Monte-Carlo comparison and an application. J. Statist. Comput. and Simul. 90:10, 1735– 1752
- [184] GOUVEIA-REIS D (2014). Statistical Modelling of Extreme Rainfall in Madeira Island. Tese de Doutoramento, Universidade da Madeira.
- [185] HAAN L DE (1970). On Regular Variation and its Application to the Weak Convergence of Sample Extremes. PhD Thesis, Mathematical Centre Tract 32, Amsterdam.
- [186] HAAN L DE (2006). Discussion of "Copulas: Tales and facts", by Thomas Mikosch. Extremes 9, 21–22.
- [187] HAAN L DE (2015). Convergence of heteroscedastic extremes. Statistics and Probability Letters 101, 38–39.
- [188] HAAN L DE and FERREIRA A (2006). Extreme Value Theory: An Introduction. Springer Science + Business Media, LLC, New York.
- [189] HAAN L DE and LIN T (2001). On convergeance towards an extreme value distribution in C[0,1]. Annals of Prob. 29, 467–483.
- [190] DE HAAN L and ZHOU C (2008). On extreme value analysis of a spatial process. *Revstat—Statist. Journal* **6**:1, 71–81.
- [191] HAAN L DE and ZHOU C (2011) Extreme residual dependence for random vectors and processes. Advances in Applied Probability 43:1, 217–242.
- [192] HAAN L DE, LI D, PENG L and IGLÉSIAS PEREIRA H (2002). Alternative conditions for attraction to stable vectors. Probab. Math. Statist. 22:2, 303–317.
- [193] HAAN, L. DE, VRIES, C.G. DE and ZHOU, C. (2009). The expected payoff to Internet auctions. *Extremes* 12, 219–238.
- [194] HAAN L DE, VRIES CG DE and ZHOU C (2013). The number of active bidders in Internet auctions, *Journal of Economic Theory* 148, 1726–1736.
- [195] HAAN L DE, KLEIN TANK A and NEVES C (2015). On tail trend detection: modeling relative risk. *Extremes* 18,141–178.
- [196] HAAN L DE, MERCADIER C and ZHOU C (2016). Adapting extreme value statistics to financial time series: dealing with bias and serial dependence. *Finance and Stochastics* 20, 321–354.
- [197] HALL A (1996). Maximum term of a particular sequence with discrete margins. Communications in Statistics—Theory and Methos 25, 721–736.
- [198] HALL A (1998). Extremos de Sucessões de Contagem Do Outro Lado do Espelho. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [199] HALL, A. (2001). Extremes of moving average models with regularly varying tails. *Extremes* 4:3, 219–239.
- [200] HALL, A. (2003). Extremes of integer-valued moving average models with exponential type tails. *Extremes* 6 (4), 361–379.
- [201] HALL A and SCOTTO M (2006). Extremes of periodic integer-valued sequences with exponential type tails. *Revstat—Statist. J.* 4:3, 249–273.
- [202] HALL, A. and SCOTTO, M.G. (2008). On the extremes of randomly sub-sampled time series, *Revstat—Statist. J.*, 6, 2, 151–164.
- [203] HALL A, GOMES MI, ROOTZEN H and SCOTTO M, Eds. (2004a). Book of Abstracts: 3rd International Symposium on Extreme Value Analysis—Theory and Practice. Universidade de Aveiro Editions, ISBN: 972-789-131-4 (130 pages).
- [204] HALL A, SCOTTO M and FERREIRA H (2004b). On the extremal behaviour of generalised periodic sub-sampled moving average models with regularly varying tails. *Extremes* 7:2, 149– 160.

- [205] HENRIQUES-RODRIGUES L (2009). Estimação de Viés Reduzido em Estatística de Extremos. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [206] HENRIQUES-RODRIGUES L and GOMES MI (2009). High quantile estimation and the PORT methodology, *Revstat—Statist. J.* 7(3), 245–264.
- [207] HENRIQUES-RODRIGUES L and GOMES MI (2018). Location invariant reduced-bias tail index estimation under a third-order framework. J. Statist. Theory and Practice 12:2, 206–230.
- [208] HENRIQUES-RODRIGUES L, GOMES MI and PESTANA DD (2011). Statistics of extremes in athletics. Revstat—Statist. J. 9:2, 127–153.
- [209] HENRIQUES-RODRIGUES L, GOMES MI, FRAGA ALVES MI and NEVES C (2014). PORT estimation of a shape second-order parameter. *Revstat—Statist. J.* 12:3, 299–328.
- [210] HENRIQUES-RODRIGUES L, GOMES MI and MANJUNATH BG (2015). Estimation of a scale second-order parameter related to the PORT methodology. *Journal of Statistical Theory and Practice* 9:3, 571–599.
- [211] IGLÉSIAS PEREIRA H (1983). Rate of convergence towards a Fréchet type limit distribution. Ann. Sci. Univ. Clermont-Ferrand II Probab. Appl. 1, 67–80.
- [212] JACOB D, NEVES C and GREETHAM DV (2020). Forecasting and Assessing Risk of Individual Electricity Peaks. Springer Briefs in Mathematics of Planet Earth.
- [213] KITSOS C, OLIVEIRA T AND STHELIK M, Eds. (2016). Special Issue on 'Risk Analysis: Challenges and Applications', *Revstat—Statist. J.* 14:2, Instituto Nacional de Estatística.
- [214] LEIVA V, FERREIRA M, GOMES MI and LILLO C (2016). Extreme value Birnbaum-Saunders regression models applied to environmental data. SERRA: Stochastic Environmental Research and Risk Assessment 30:3,1045–1058.
- [215] LEIVA V, CAMILLO L, GOMES MI and FERREIRA M (2019). Discussion of "Birnbaum-Saunders distribution: A review of models, analysis, and applications" and a novel financial extreme value data analytics from natural disasters. *Applied Stochastic Models in Business* and Industry 35:1, 90–95.
- [216] LENG X, PENG L, WANG X and ZHOU C (2019). Endpoint estimation for observations with normal measurement errors. *Extremes* 22:1,71–96.
- [217] LI D (2004). On Extreme Value Approximation to Tails of Distribution Functions. PhD Thesis, Tinbergen Institute, University of Rotterdam.
- [218] LIMA DE SOUZA A (2017). Cota Superior de Grandes Desvios para Sumidouros Hiperbólicos Singulares. Tese de Doutoramento, Universidade Federal da Bahia.
- [219] LIN T (2002). Statistics of Extremes in the Space of Continuous Functions. PhD Thesis, Erasmus University Rotterdam.
- [220] LOMBA JS and FRAGA ALVES MI (2020). L-moments for automatic threshold selection in extreme value analysis. SERRA: Stochastic Environmental Research and Risk Assessment 34, 465–491.
- [221] LUCARINI V, FARANDA D, FREITAS ACM, FREITAS JM, KUNA T, HOLLAND D, NICOL D, TODD D and VAIENTI S (2016). Extremes and Recurrence in Dynamical Systems. Hoboken, N.J., Wiley.
- [222] MARTINS AP (2005). *Coeficientes Extremais*. Tese de Doutoramento, Departamento de Matemática, Universidade da Beira Interior.
- [223] MARTINS AP and FERREIRA H (2004a). The extremal index of sub-sampled processes. J. Statistical Planning and Inference 124:1, 145–152.
- [224] MARTINS AP and FERREIRA H (2004b). Extremes of periodic moving averages of random variables with regularly varying tail probabilities. SORT 28:2, 165-175.
- [225] MARTINS MJ (2001). Estimação de Caudas Pesadas Variantes ao Estimador de Hill. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.

- [226] MARTINS MJ, GOMES MI and NEVES MM (1999). Some results on the behaviour of Hill's estimator. J. Statist. Comp. and Simulation 63, 283-297.
- [227] MENDONÇA S (2001). Tópicos Sobre a Convergência Fraca de Sucessões de Variáveis Aleatórias. Tese de Doutoramento, Universidade da Madeira.
- [228] MIGUÉNS MF (2004). Modelo Bivariado para Caudais Máximos. Tese de Doutoramento, Universidade Nova de Lisboa.
- [229] MIRANDA MC (2005). Estatística de Extremos: Estimação dos Índices Extremal e de Cauda. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [230] MONTFORT MAJ VAN and GOMES MI (1985). Statistical choice of extremal models for complete and censored data. J. Hydrology 77, 77–87.
- [231] NEVES C (2006). Estimation and Testing for Distributions with Light, Heavy and Superheavy Tails. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [232] NEVES C and FRAGA ALVES MI (2004). Reiss and Thomas' automatic selection of the number of extremes. *Comput. Statist. Data Anal.* 47:4, 689-704.
- [233] NEVES C and FRAGA ALVES MI (2008). Testing extreme value conditions—an overview and recent approaches, *Revstat—Statist. J.* **6**:1, 83–100.
- [234] NEVES C, PICEK J and FRAGA ALVES MI (2006). The contribution of the maximum to the sum of excesses for testing max-domains of attraction. J. Statist. Planning and Inference 136:4, 1281–1301.
- [235] NEVES C, GOMES MI and FRAGA ALVES MI (2011). Extreme nitriding limits in aluminum extrusion. International Journal of Mathematical Modelling and Numerical Optimisation (IJMMNO) 2:3, 342–355.
- [236] NEVES MM (1990). Estimação por Blocos dos Parâmetros de Distribuição Fréchet. Comparação de Métodos Expeditos. Tese de Doutoramento, Faculdade de Ciências e Tecnologia, Universidade Nova de Lisboa.
- [237] NEVES MM, GOMES MI, FIGUEIREDO F and PRATA-GOMES D (2015). Modeling extreme events: sample fraction adaptive choice in parameter estimation. *Journal of Statistical Theory* and Practice 9:1, 184–199.
- [238] NUNES SA, DA CAMARA CC, TURKMAN KF, CALADO TJ. TRIGO RM and AMARAL TURKMAN MA (2019). Wildland fire potential outlooks for Portugal using meteorological indices of fire danger. *Nat. Hazards Earth Syst. Sci.* 19, 1459–1470.
- [239] OLIVEIRA A, OLIVEIRA TA and SEIJAS-MACIAS A (2016). Skewness into the product of two normally distributed variables and the risk consequences. *Revstat–Statist. J.* 14:2, 119–138.
- [240] OLIVEIRA MF (1992). Leis Limites em Sucessões Dependentes de uma Cadeia. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [241] OLIVEIRA MF and TURKMAN KF (1992). A note on the asymptotic independence of maximum and minimum of stationary sequences with extremal index. *Portugal. Math.* 49:1, 29–36.
- [242] OLIVEIRA O (2003). In Extremis. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [243] OLIVEIRA O, GOMES MI and FRAGA ALVES MI (2006). Improvements in the estimation of a heavy tail. *Revstat-Statist. J.* 4:2, 81-109.
- [244] OLIVEIRA T, GOMES MI, KITSOS C, OLIVEIRA A and GRILO L, Eds. (2013). Book of Abstracts—7th Workshop on Statistics, Mathematics and Computation and 5th International Conference on Risk Analysis. Instituto Nacional de Estatística (INE) editions, ISBN:978-972-9473-71-5. Depósito Legal: 359956/13 (191 pages).

- [245] OLIVEIRA T, OLIVEIRA A, GRILO LM, CARAPAU F, DIAS C and SANTOS C, Eds. (2017). Book of Abstracts—Satellite Meeting ISI-Committee on Risk Analysis and XI Workshop on Statistics, Mathematics and Computation. IPP–Instituto Politécnico de Portalegre editions, ISBN:978-989-8806-18-5. (132 pages).
- [246] PEKALP MH, AYDOGDU H and TURKMAN KF (2019). Discriminating between some lifetime distributions in geometric counting processes. *Communications in Statistics—Simul. and Computation.* On-line: Sept. 11, 2019. DOI: 10.1080/03610918.2019.1657452.
- [247] PENALVA H (2017). Contributos Computacionais e Metodológicos na Estimação de Valores Extremos. Tese de Doutoramento, Instituto Superior de Agronomia, Universidade de Lisboa.
- [248] PENALVA H, NEVES MM and NUNES S (2013). Topics in Data Analysis Using R in Extreme Value Theory. Advances in Methodology and Statistics 10:1, 17–29.
- [249] PENALVA H, NUNES S and NEVES MM (2016). Extreme value analysis A brief overview with an application to flow discharge rate data in a hydrometric station in the north of Portugal. *Revstat—Statist. J.* 14:2, 193–215.
- [250] PENALVA H, PRATA GOMES D, NEVES MM and NUNES S (2019). Testing conditions and estimating parameters in extreme value theory: application to environmental data *Revstat–Statist. J.* 17:2, 187–207.
- [251] PENALVA H, GOMES MI, CAEIRO F and NEVES MM (2020a). A couple of non-reduced bias generalized means in extreme value theory: an asymptotic comparison. *Revstat—Statist. J.* 18:3, 281–298.
- [252] PENALVA H, GOMES MI, CAEIRO F and NEVES MM (2020b). Lehmer's mean-of-order-p extreme value index estimation: a simulation study and applications. J. Applied Statistics 47:13-15 (Advances in Computational Data Analysis), 2825–2845.
- [253] PEREIRA JMC, OOM D, PEREIRA P, AMARAL TURKMAN MA and TURKMAN KF (2015). Religious Affiliation Modulates Weekly Cycles of Cropland Burning in Sub-Saharan Africa. PLOS one. 10:9:, DOI: 10.1371/journal.pone.0139189
- [254] PEREIRA JMC, AMARAL TURKMAN MA, TURKMAN KF and OOM D (2019). Anthromes displaying evidence of weekly cycles in active fire data cover 70% of the global land surface. *Scientific Reports* 9 (11424).
- [255] PEREIRA ML (2002). Valores Extremos Multidemensionais de Variáveis Dependentes. Tese de Doutoramento, Universidade da Beira Interior.
- [256] PEREIRA ML (2004). Extremal behaviour in models of superposition of random variables. *Revstat—Statist. J.* 2:2, 163-178.
- [257] PEREIRA ML and FERREIRA H (2001). Limit distribution for point processes of high local maxima. J. Statistical Planning and Inference 97, 227–233.
- [258] PEREIRA ML, MARTINS AP and FERREIRA H (2017). Clustering of high values in random fields. *Extremes* 20:4, 807–838.
- [259] PEREIRA P (2014). Métodos Probabilísticos e Estatísticos na Gestão de Fogos Florestais. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [260] PEREIRA P, TURKMAN KF, AMARAL TURKMAN MA, SÁ A and PEREIRA JMC (2013). Quantification of annual wildfire risk; A spatio-temporal point process approach. *Statistica* 73, 55–68.
- [261] PEREIRA S (2018). Spatio-temporal Methods and Models for Unemployment Estimation. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [262] PEREIRA S, TURKMAN KF and CORREIA L (2018). Spatio-temporal analysis of regional unemployment rates: A comparison of model-based approaches. *Revstat—Statist. J.* 16:4, 515–536.
- [263] PEREIRA S, MENEZES R, ANGÉLICO MM and MARQUES T. (2020). Geostatistical models for zero-inflated data and extreme values. ArXiv:2010.12474.

- [264] PINTO MM, DA CAMARA C, TRIGO IF, TRIGO RM and TURKMAN KF (2018). Fire danger rating over mediterranean europe based on fire radiative power derived from meteosat. *Natural Hazards and Earth System Sciences* 18, 515–529.
- [265] PRATA GOMES, D (2008). Métodos Computacionais na Estimação Pontual e Intervalar do Índice Extremal. Tese de Doutoramento, Faculdade de Ciências e Tecnologia, Universidade Nova de Lisboa.
- [266] RAMOS A (2003). Multivariate Joint Tail Modelling and Score Tests of Independence. PhD Thesis, Surrey University.
- [267] RAMOS A and LEDFORD AW (2005). Regular score tests of independence in multivariate extreme values. *Extremes* 8:1, 5-26.
- [268] REIS P (2012). Modelos Limite para a Fiabilidade de Sistemas de Grande Dimensão. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [269] REIS P and CANTO E CASTRO, L (2009). Limit model for the reliability of a regular and homogeneous series-parallel system. *Revstat—Statist. J.* 7, 227–243.
- [270] REIS P, CANTO E CASTRO L, DIAS S and GOMES MI (2015). Penultimate approximations and reliability of large coherent systems. *Methodology and Computing in Applied Probability* 17:1, 189–206.
- [271] SCOTTO MG (2001). On the Extremes of Certain Time Series. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [272] SCOTTO MG (2007). Extremes for solutions to stochastic difference equations with regularly varying tails. *Revstat—Statist. J.* 5:3, 229–247.
- [273] SCOTTO MG and GUEDES SOARES C (2000). Modelling the long-term series of significant wave heights with non-linear threshold models. *Coastal Engineering* **40**, 313-327.
- [274] SEBASTIÃO JR (2013). Índice de Cruzamentos: Propriedades e Inferência. Tese de Doutoramento em Matemática Aplicada, Universidade da Beira Interior.
- [275] SEBASTIÃO JR, MARTINS AP, PEREIRA ML and FERREIRA H (2010). Clustering of upcrossings of high values. J. Statistical Planning and Inference 140:4, 1003–1012.
- [276] SILVA AT (2017). Nonstationarity and Uncertainty of Extreme Hydrological Events. PhD Thesis in Civil Engineering, IST, ULisboa.
- [277] SILVA AT and PORTELA MM (2012). Disaggregation modelling of monthly streamflows using a new approach of the method of fragments. *Hydrological Sciences J.* 57:5, 1–14.
- [278] SILVA AT, PORTELA MM and NAGHETTINI M (2012). Nonstationarities in the occurrence rates of flood events in Portuguese watersheds. *Hydrology and Earth System Sciences* 16, 241–254.
- [279] SILVA AT, PORTELA MM and NAGHETTINI M (2014). On peaks-over-threshold modeling of floods with zero-inflated-Poisson arrivals under stationarity and nonstationarity. *Stochastic Environmental Research and Risk Assessment* 28:6, 1587–1599.
- [280] SILVA AT, NAGHETTINI M and PORTELA MM (2016). On some aspects of peaks-overthreshold modeling of floods under nonstationarity using climate covariates. *Stochastic En*vironmental Research and Risk Assessment **30**:1, 207–224.
- [281] SILVA I and SILVA ME (2009). Parameter Estimation for INAR Processes Based on High-Order Statistics. *Revstat—Statist. J.* 7:1, 105–117.
- [282] SOUSA BC DE (2002). A Contribution to the Estimation of the Tail Index of Heavy-Tailed Distributions. PhD Thesis, University of Michigan.
- [283] SOUSA PM, BARRIOPEDRO D, TRIGO RM, RAMOS AM, NIETO R, GIMENO L, TURK-MAN KF and LIBERATO DLR (2016). Impact of Euro-Atlantic blocking patterns in Iberia precipitation using a novel high-resolution dataset. *Clim Dyn.* 46: 2573.
- [284] SOUSA COSTA E (2015). Análise de Precipitações Intensas e de Caudais Extremos em Países com Economias Emergentes de Rápido Desenvolvimento. Aplicação a Angola. Tese de Doutoramento, Instituto Superior Técnico, Universidade de Lisboa.

- [285] TEMIDO MG (1999). Maxima and minima of stationary random sequences under a local dependence restriction. *Portugal. Math.* 56:1, 59–72.
- [286] TEMIDO MG (2000). Classes de Leis Limites em Teoria de Valores Extremos Estabilidade e Semiestabilidade. Tese de Doutoramento, Universidade de Coimbra.
- [287] TEMIDO MG and FERREIRA H, Eds. (2002). Extreme Values and Resampling Techniques, Universidade de Coimbra and CEAUL editions.
- [288] THEMIDO PEREIRA T (1994). Contribuições à Teoria de Valores Extremos. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [289] TIAGO DE OLIVEIRA J (1975). Bivariate and Multivariate Extreme Distributions. In G. P. Patil et al., NATO ASI Statistical Distributions in Scientific Work, Dordrecht; D. Reidel eds., 355–361.
- [290] TIAGO DE OLIVEIRA J (1977a). Asymptotic Distributions of Univariate and Bivariate m-th Extremes. in J. R. Barra *et al.* (eds.), *Recent Developments in Statistics*, North-Holland, 613–617.
- [291] TIAGO DE OLIVEIRA J (1977b). Estimation for Gumbel Bivariate Model. Rev. Roumaine Math. Pures Appl., XXII, 71141–145.
- [292] TIAGO DE OLIVEIRA J (1977c). Statistic Methodology for Large Claims. The ASTIN Bull, IX, 1–9.
- [293] TIAGO DE OLIVEIRA J (1978a). Approximate Distributions for Sequences of Maxima. Metron XXXVI, 3–21.
- [294] TIAGO DE OLIVEIRA J (1978b). Extremos Bivariados: Modelos e Perspectivas. Mem. Acad. Ciências de Lisboa, Classe Ciências, XXII, 371–386.
- [295] TIAGO DE OLIVEIRA J (1981). Statistical choice of univariate extreme models. In C. Taillie et al. (eds.), Statistical Distributions in Scientific Work, Vol. 6, 367-387.
- [296] TIAGO DE OLIVEIRA J (1982a). A definition of estimator efficiency in k-parameter case. Ann. Inst. Statist. Math. 34:3, 411–421.
- [297] TIAGO DE OLIVEIRA J (1982b). Decision and modelling for extremes. In Some Recent Advances in Statistics, 101–110, Academic Press, London.
- [298] TIAGO DE OLIVEIRA J (1982c). Efficient Estimation for Quantiles of Weibull Distributions, *Rev. Belge Statist. Rech. Oper.* 22:4, 3–10.
- [299] TIAGO DE OLIVEIRA J (1982d). The δ -method for obtention of asymptotic distributions; applications. *Publ. Inst. Statist. Univ. Paris*, Vol. **XXVII**, 49–70.
- [300] TIAGO DE OLIVEIRA J (1983). Gumbel Distribution. In N. L. Johnson and S. Kotz (eds.), Encyclopedia of Statistical Sciences III, 552-558, New York, Wiley.
- [301] TIAGO DE OLIVEIRA J, Ed. (1984a). Statistical Extremes and Applications. NATO Advanced Science Institutes Series C: Mathematical and Physical Sciences, 131. D. Reidel, Dordrecht.
- [302] TIAGO DE OLIVEIRA J (1984b). Bivariate models for extremes; statistical decision. In Tiago de Oliveira ed., Statistical Extremes and Applications, 131–153, D. Reidel, Dordrecht.
- [303] TIAGO DE OLIVEIRA J (1984c). Initiation of Statistical Decision for Weibull Distributions, Proc. XII Reunión Nacional SEIO, in Cuadernos Bioestadist. Aplic. Informat. 2, 495–499.
- [304] TIAGO DE OLIVEIRA J (1984d). Univariate extremes: statistical choice. In Tiago de Oliveira J (ed.), Statistical Extremes and Application, 91-107, D. Reidel, Dordrecht.
- [305] TIAGO DE OLIVEIRA J (1984e). Weibull Distributions and Large Earthquake Modelling. In S. Eggwertz e N. C. Lind (eds.), *Probabilistic Methods in the Mechanics of Solids and Structures*, IUTAM symposium in honor of Doctor W. Weibull, 81-89, Stockholm,
- [306] TIAGO DE OLIVEIRA J and EPSTEIN, B, Eds. (1982). Some Recent Advances in Statistics. Academic Press, Inc. [Harcourt Brace Jovanovich, Publishers], London.
- [307] TIAGO DE OLIVEIRA J and GOMES MI (1984). Two test statistics for choice of univariate extreme models. In Tiago de Oliveira J (ed.), *Statistical Extremes and Application*, 651-668, D. Reidel, Dordrecht.

- [308] TURKMAN KF (1980). Limiting Distribution of Maxima of Certains Types of Non-Stationary Stochastic Processes. PhD Thesis, University of Sheffield.
- [309] TURKMAN KF (1982). On the asymptotic Poisson behaviour of the upcrossings of trigonometric polynomials with random coefficients. In Proceedings of the Ninth Spanish-Portuguese Conference on Mathematics 2, 725–727, Acta Salmanticensia. Ciencias 46, Univ. Salamanca, Salamanca.
- [310] TURKMAN KF (1984a). Degenerate limit laws for the maxima of trigonometric polynomials with random coefficients. *Portugal. Math.* 42:4, 355–369 (1986).
- [311] TURKMAN KF (1984b). On the asymptotic upcrossings of a class of nonstationary sequences. In Tiago de Oliveira (ed.), *Statistical Extremes and Applications*, 669–678, D. Reidel, Dordrecht.
- [312] TURKMAN KF (2014). On the upcrossings of trigonometric polynomials with random coefficients. *Revstat—Statist. J.* 12:2, 135–155.
- [313] TURKMAN KF and OLIVEIRA MF (1992). Limit laws for the maxima of chain-dependent sequences with positive extremal index. J. Appl. Probab. 29:1, 222–227.
- [314] TURKMAN KF and WALKER AM (1983). Limit laws for the maxima of a class of quasistationary sequences. J. Appl. Probab. 20:4, 814–821.
- [315] TURKMAN KF and WALKER AM (1984). On the asymptotic distributions of maxima of trigonometric polynomials with random coefficients. *Adv. in Appl. Probab.* **16**:4, 819–842.
- [316] TURKMAN KF, AMARAL TURKMAN MA and PEREIRA P (2010). Asymptotic models and inference for extremes of spatio-temporal data. *Extremes* 13:4, 375–397.
- [317] TURKMAN KF, DE HAAN L and AMARAL TURKMAN MA, Eds. (2013). Symposium on Recent Advances in Extreme Value Theory: Book of Abstracts. CEAUL editions.
- [318] TURKMAN KF, AMARAL TURKMAN MA, PEREIRA P, SÁ A and PEREIRA JMC (2014a). Generating annual fire risk maps using Bayesian hierarchical models. *Journal of Statistical Theory and Practice* 8:3, 509–533.
- [319] TURKMAN KF, SCOTTO D and DE ZEA BERMUDEZ P (2014b). Non-linear Time Series: Extreme Events and Integer Value Problems. Springer, Heidelberg.
- [320] URSU E and TURKMAN KF (2012). Periodic autoregressive model identification using genetic algorithms. J. of Time Series 33, 398–405.
- [321] VALENTE DE FREITAS MA (1998). Nova Classe de Aproximações em Teoria de Valores Extremos, Tese de Doutoramento, Universidade de Aveiro.
- [322] VALENTE DE FREITAS AND HÜSLER (2003). Condition for the convergence of maxima of random triangular arrays. *Extremes* **6**, 391–394.
- [323] VELTHOEN J, CAI J-J, JONGBLOED G and SCHMEITS M (2019). Improving precipitation forecasts using extreme quantile regression. *Extremes* 22:4, 599–622.
- [324] VISEU C (2011). *Extremos Multivariados*. Doutoramento em Matemática, Univiersidade da Beira Interior.
- [325] VRIES CG DE and ZHOU C (2006). Discussion of "Copulas: Tales and facts", by Thomas Mikosch. Extremes 9, 23–25.
- [326] ZEA BERMUDEZ, PATRÍCIA DE (2003). Bayesian Approach to Extreme Quantile Estimation. Tese de Doutoramento, DEIO, Faculdade de Ciências, Universidade de Lisboa.
- [327] ZEA BERMUDEZ P, AMARAL TURKMAN MA and TURKMAN KF (2001). A predictive approach to tail probability estimation. *Extremes* 4:4, 295-314.
- [328] ZHOU C (2008a). On Extreme Value Statistics. Tinbergen Institute Research Series 432, Thela Thesis.
- [329] ZHOU C (2008b). A 2-step estimator of the extreme value index. Extremes 11:3, 281–302.
- [330] ZHOU C (2017). Book review: quantitative risk management: concepts, techniques and tools, revised edition, by A.F. McNeil, R. Frey and P. Embrechts. *Extremes* 20:2, 489–491.
- [331] ZHOU C (2018). Discussion on "Human life is unlimited but short" by Holger Rootzén and Dmitrii Zholud. Extremes 21:3, 405–410.